

NSF 2002 Summer School (Urbana-Champaign)

**Microfluidics**

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**Brown University**

- Basic Concepts and Applications
- Gas Flows
- Liquid Flows
- Particulate Flows
- Moving Domains and Applications

Reference: *G.E. Karniadakis & A. Beskok*

*Micro Flows: Fundamentals and Simulation,*  
*Springer, 2002.*

# **Microfluidics:**

***Emerging technology*** that allows development of new approaches to synthesize, purify, and rapidly screen chemicals, biologicals, and materials using integrated, massively parallel miniaturized platforms.

- **Microfluidics is *Interdisciplinary*:**
  - Micro-Fabrication
  - Chemistry
  - Biology
  - Mechanics
  - Control Systems
  - Micro-Scale Physics and Thermal/Fluidic Transport
  - Numerical Modeling
  - Material Science
  - System Integration and Packaging
  - Validation & Experimentation
  - Reliability Engineering
  - ...

# Microfluidic Devices

## Sensors & Actuators:

Pressure, Temperature, Shear Stress,  
Biological & Chemical Sensors

## Fluidic Components:

Channels, Pumps, Membranes  
Valves,  
Nozzles, Diffusers and Mixers

## Motion Generation:

Micro-Motors, Turbines,  
Steam Engines, Gears, Pistons, Links

**Micro-Total-Analysis-Systems ( $\mu$ -TAS) seamlessly integrate sample collection and separation units, biological and chemical sensors, fluid pumping and flow control elements, and electronics on a single microchip.**

# Microfluidic Applications:

## Defense Applications:

- Lab on a chip:  $\mu$ -TAS

## Bio-Medical Applications:

- Drug Delivery Systems
- DNA Analyzers
- Human Health Monitoring
- Artificial Organs

## Environmental Monitoring:

- Water & Air Pollution Sensing
- Gas/Liquid Filtration Systems

## Microelectronics:

- Thermal Management
- Bubble-Jet Printers

## Aerospace Industry:

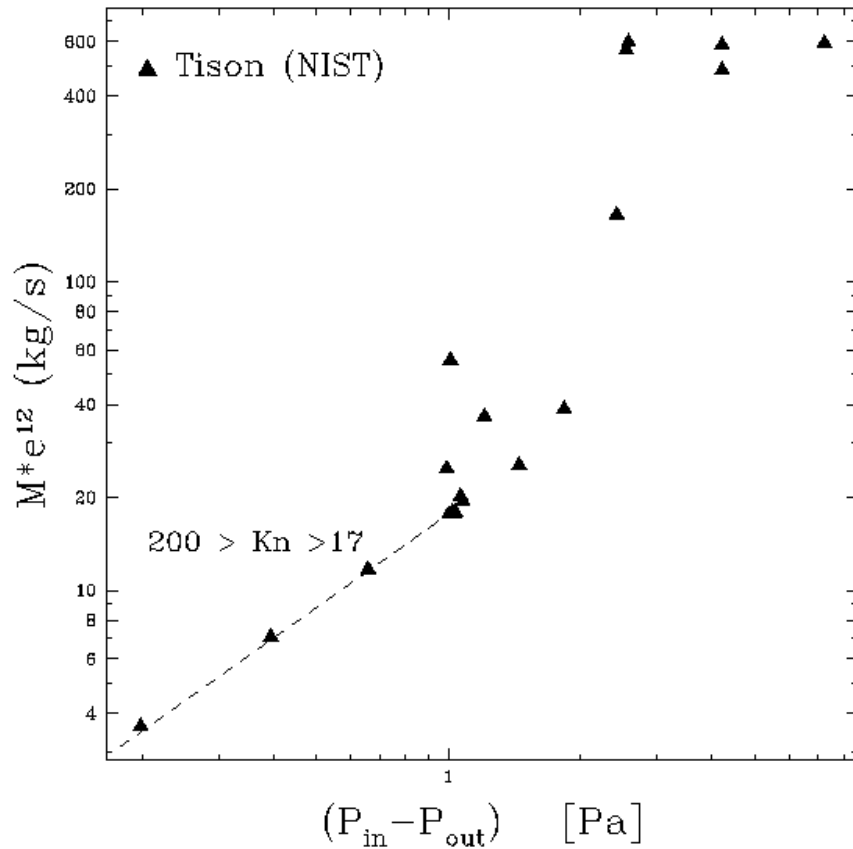
- Drag & Stall Control

# Scientific & Technological Challenges

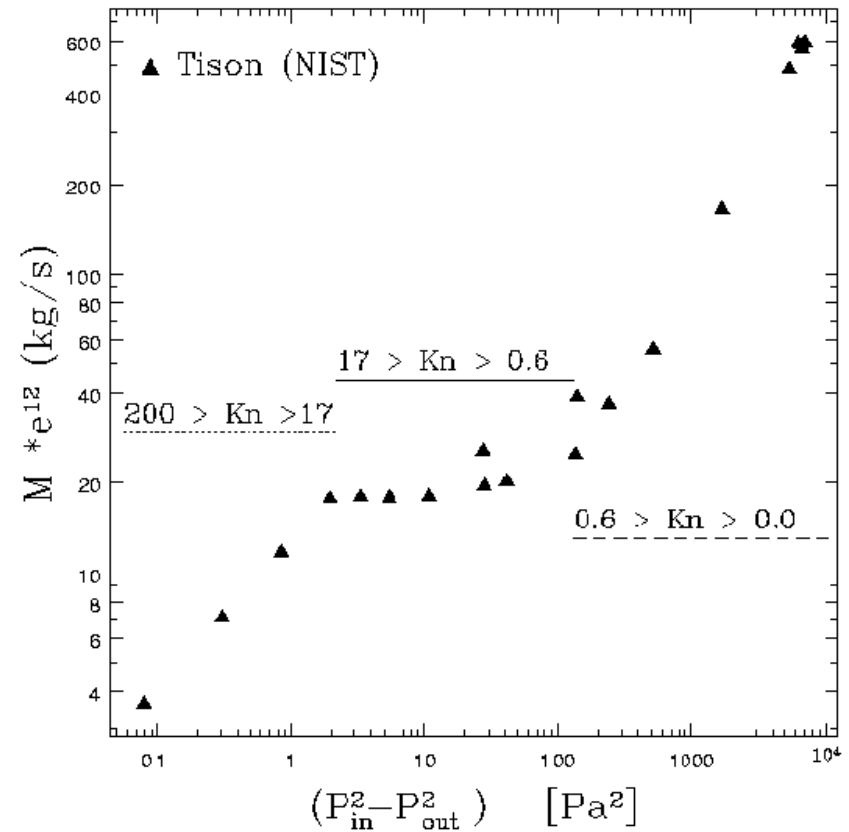
- Development of *new* concepts that are *specifically designed* to take advantage of the small scale of microfluidic devices,
- To impart unique new functions that are not simply miniaturized versions of existing systems and components.

# Mass Flow Rate versus Pressure Drop

- Pipe Flow (2mm x 200 mm; gas at low pressure)

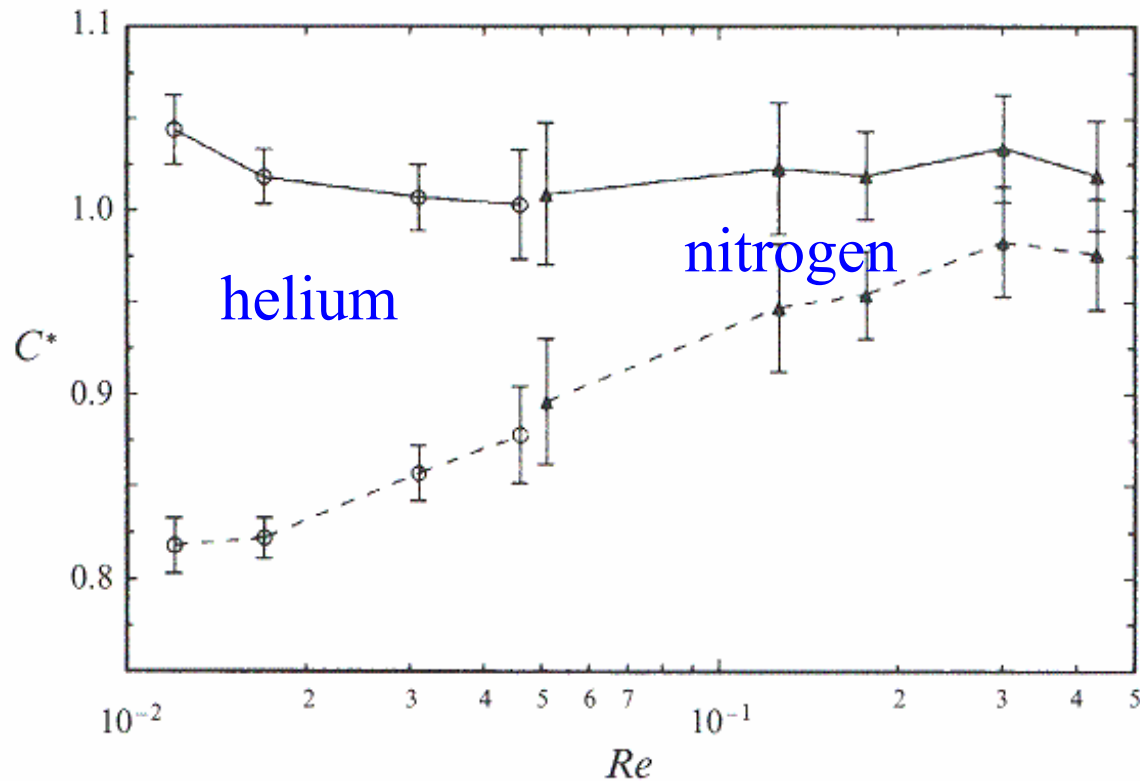


- Linear Scaling



- Quadratic Scaling

# Deviations from Continuum - Gases



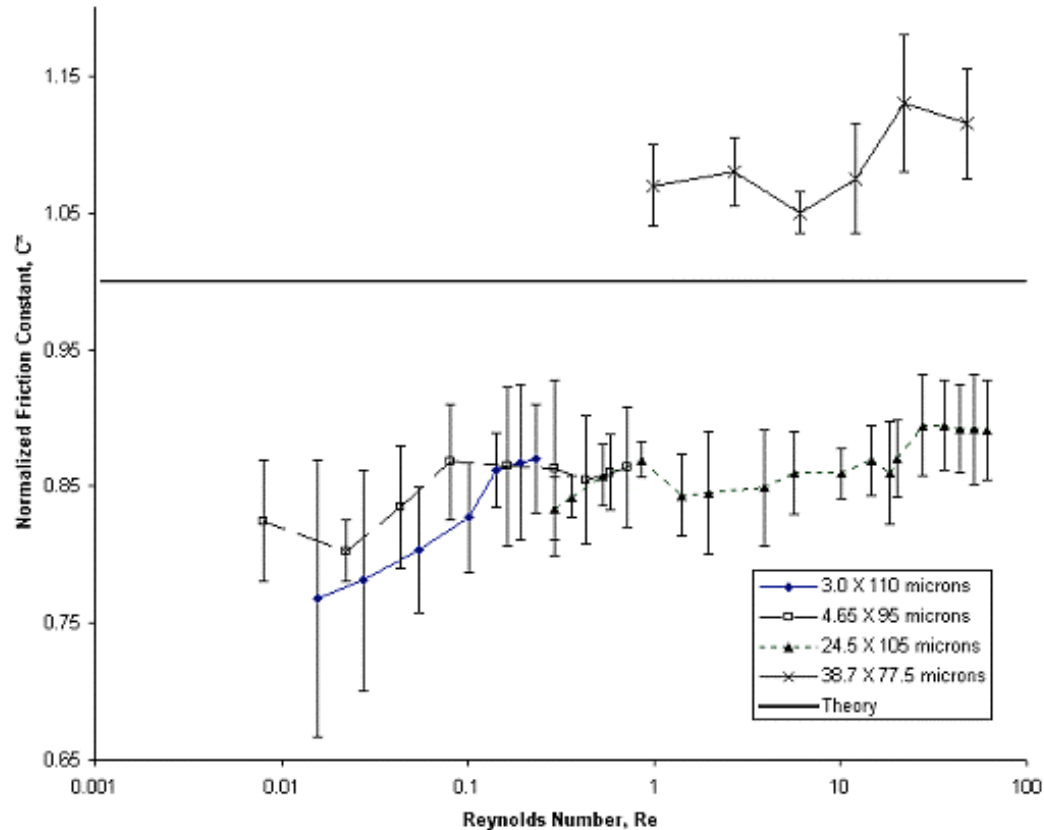
• **Microchannel:** 0.51 microns (Bau et al., U Penn, 1988)

•  $C^* = Po_{ex} / Po_{th}$  where  $Po = C_f Re$

•  $Po = 64$  (pipe)

•  $Po = 96$  (2D channel)

# Deviations from Continuum - Liquids

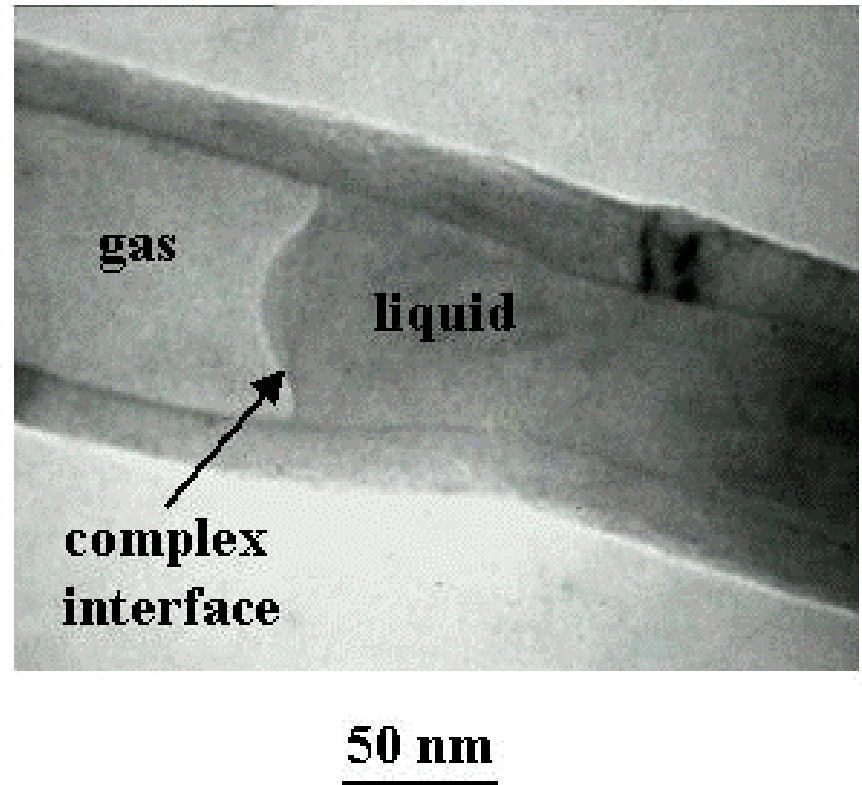
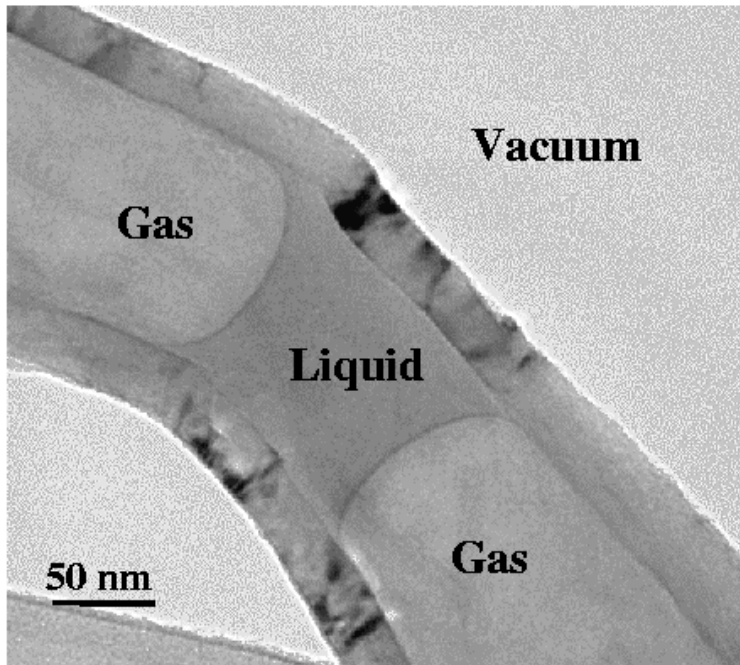


- *Microducts* (Bau & Pfahler, 2001)
- **Silicone oil**

• Question: **Anomalous Diffusion** or something else?

# Interface Inside Carbon Nano-Tubes

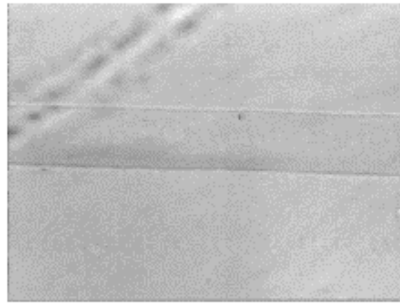
(transmission electron micrographs)



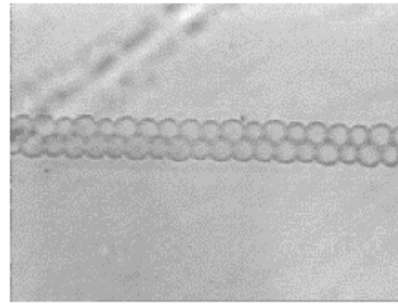
Courtesy of Megaridis & Gogotsi, UIC



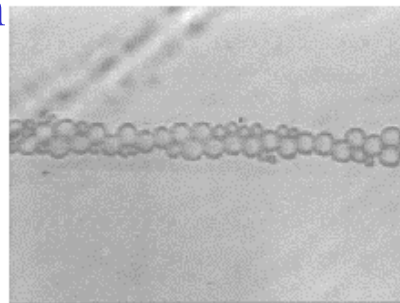
# Reverse Micelle Formation in Microchannels Containing Hexadecane/ 2% Span80



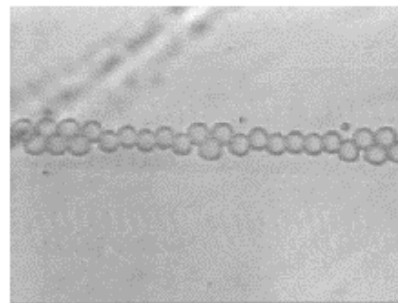
13.2/12.5 psi w/o-s



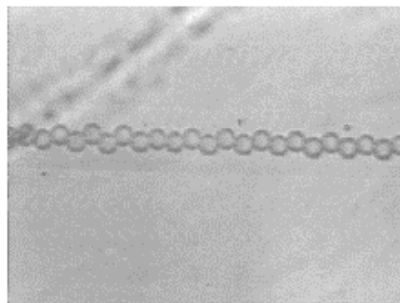
12.8/12.5 psi w/o-s



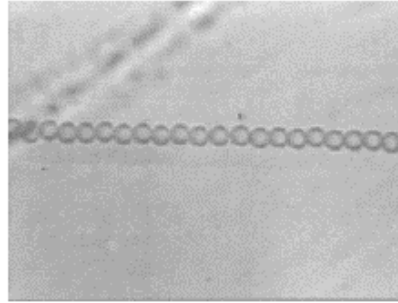
12.4/12.5 psi w/o-s



12.0/12.5 psi w/o-s



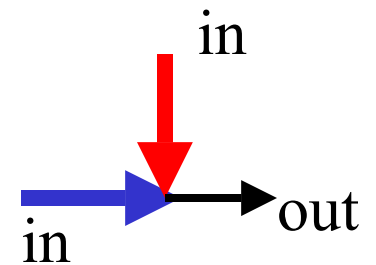
11.5/12.5 psi w/o-s



11.1/12.5 psi w/o-s

\* Quake, Caltech

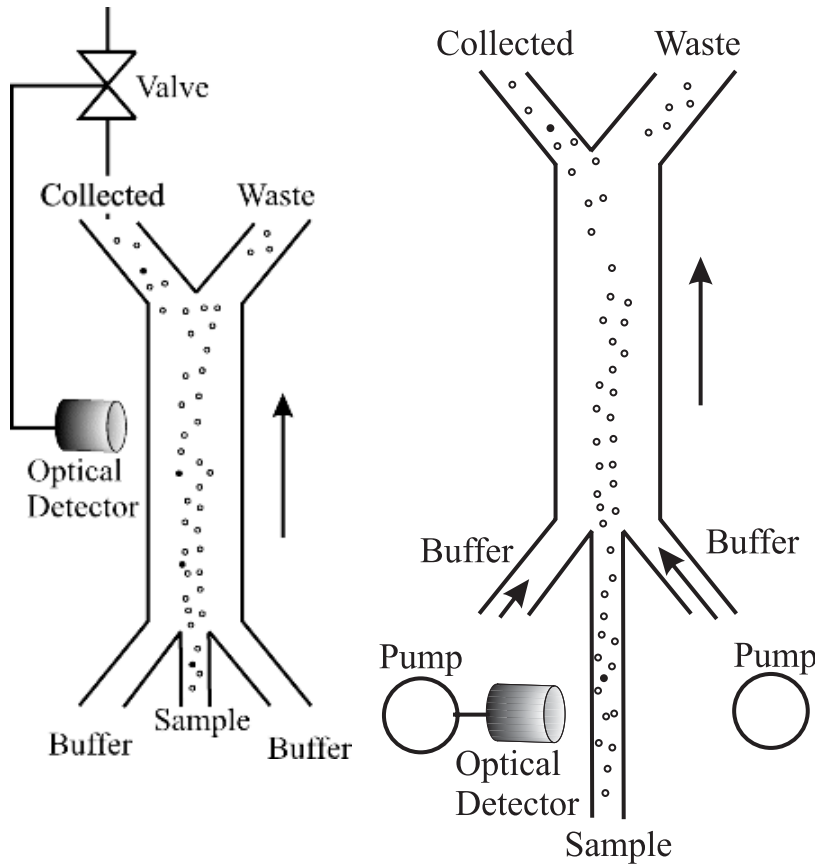
## T-junction



# Applications of Particulate Microflows

Liquids + Gas

- Sorting
  - Analyzing Of
  - Removal
- Cells
  - Particles
  - Embryos



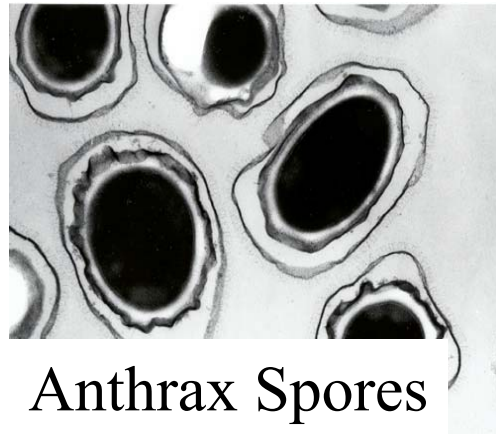
Micro magnetic activated cell sorting

$\mu$ MACS

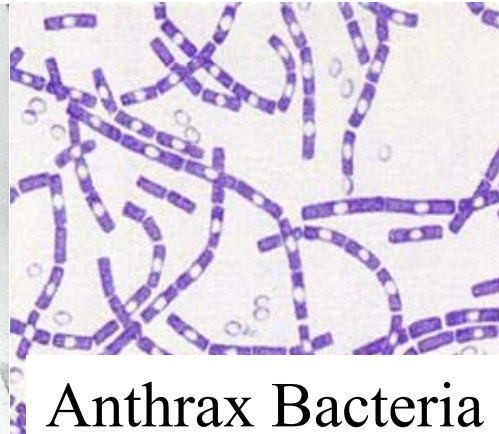
Micro fluorescent activated cell sorting  
 $\mu$ FACS

\* *Telleman et al.*

# Characterization of Airborne Particles



Anthrax Spores

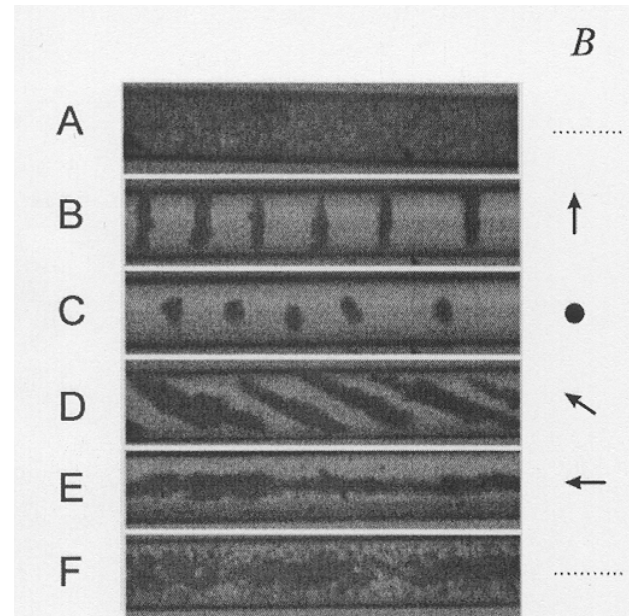
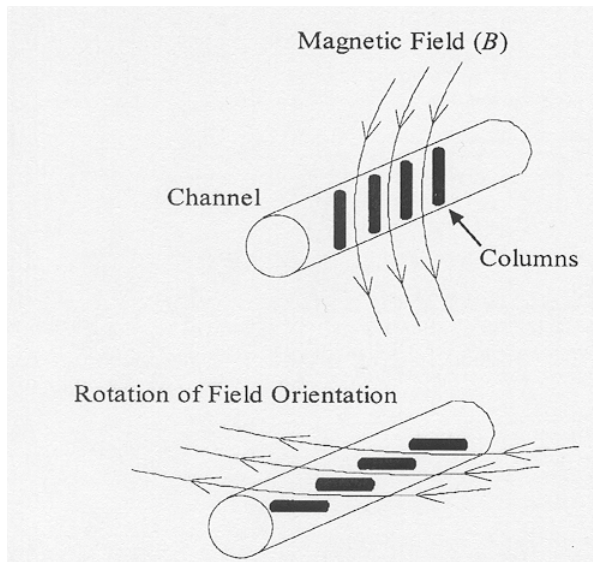


Anthrax Bacteria

**Size, Shape & Orientation**

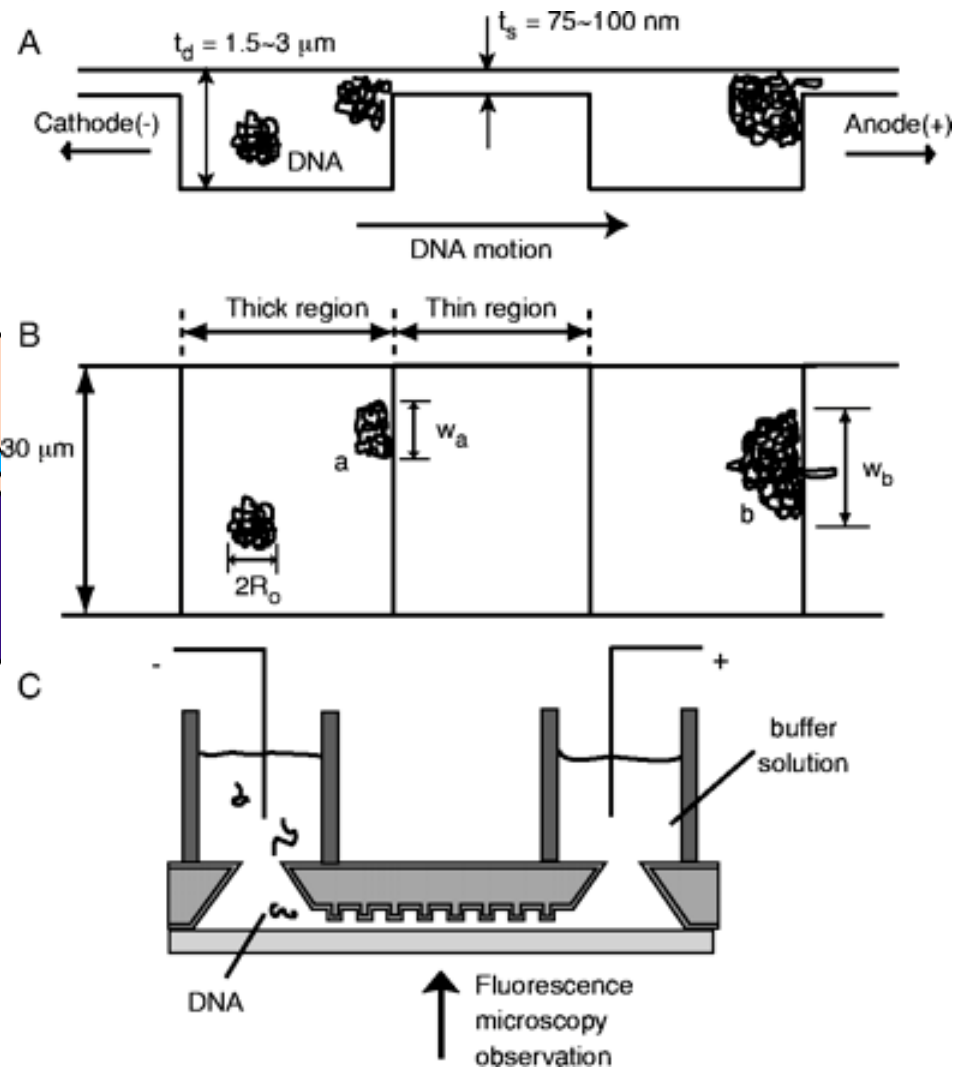
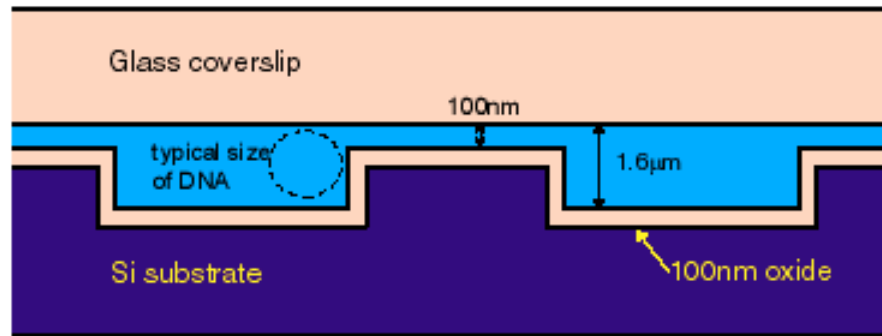
# Active Control of Supraparticle Structures Microchannels

Hayes et al. *Langmuir* (2001)



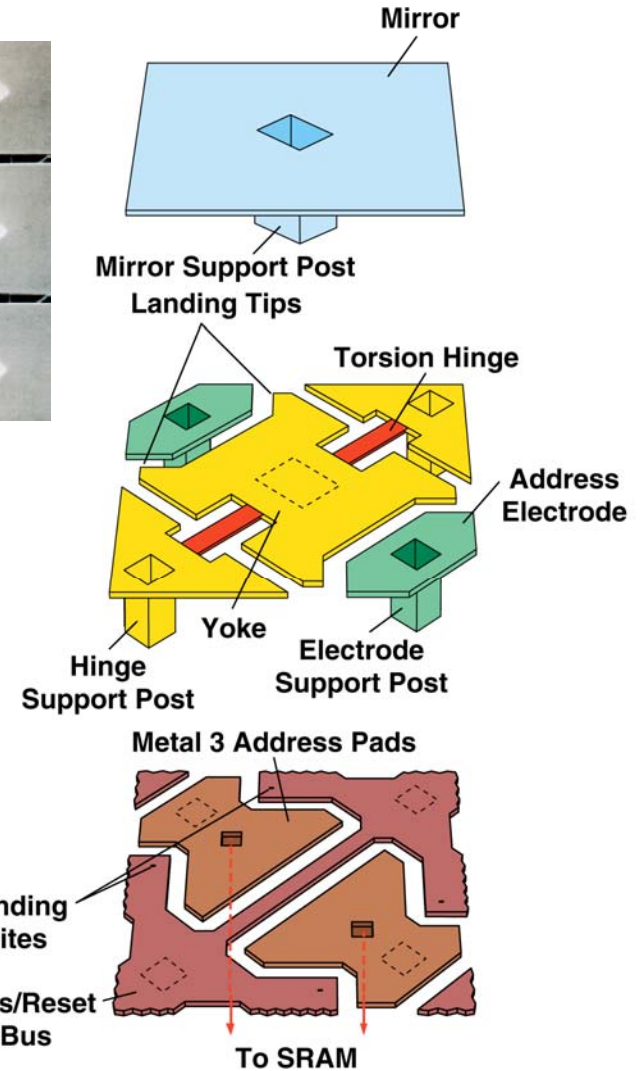
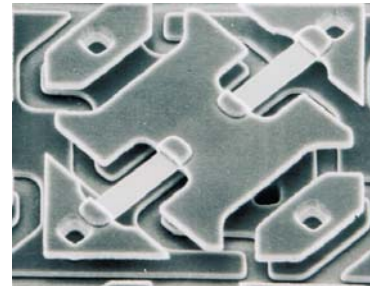
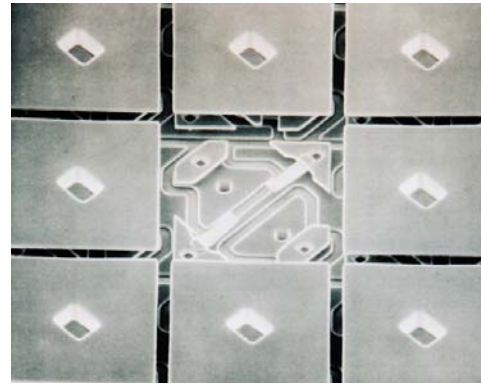
# Entropic Trapping and Seiving of DNA in Nanofluidic Channels

Han & Craighead, *Science*, (2000)



# Digital Micro-Mirror Device™

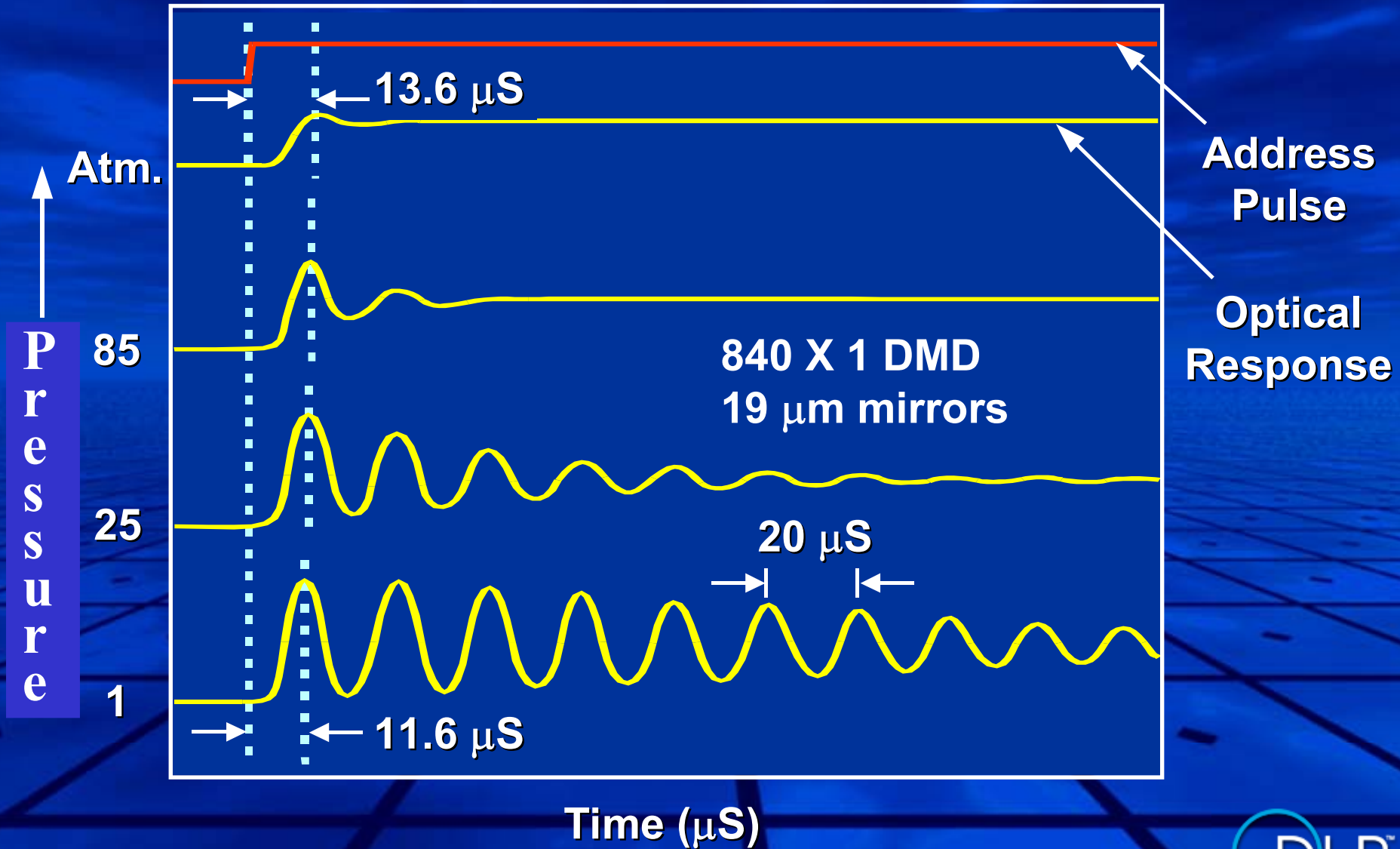
Digital Light Processing™:  
848 x 600 pixels  
1280 x 1024 pixels  
16µm x 16µm w/ 1 µm separation



Courtesy of Texas Instruments

# DMD™ Air Damping Effects & Transient Response

Courtesy of Texas Instruments

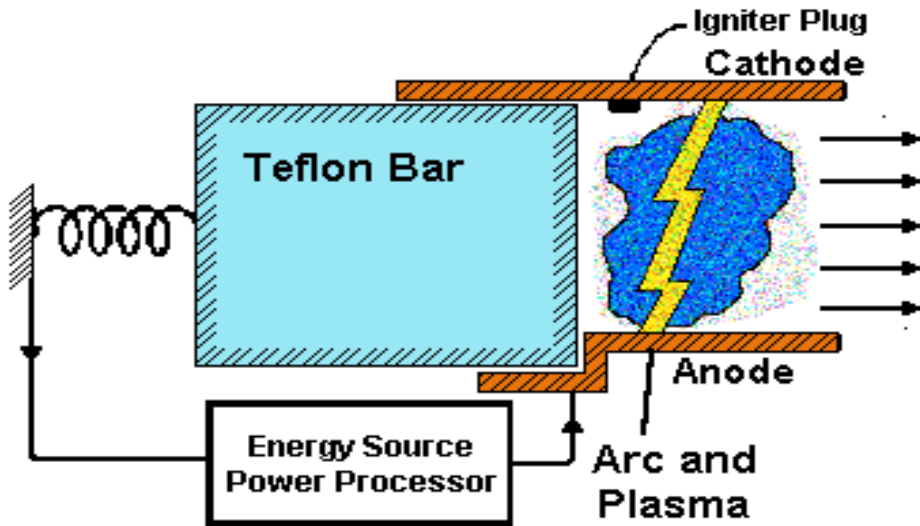


## Simulation of Micro-Pulse-Plasma Thrusters (micro-PPT)

- New issues arise in simulating plasma microthrusters that are an order of magnitude smaller than the existing state-of-the art.
  - Current simulation technologies are based on mathematical models and assumptions that break down in microscales and, therefore, cannot treat these microflows comprehensively.
- Microspaceraft are currently considered by Air Force, NASA and industry for a variety of applications.
  - $L < 10$  cm,  $W < 1$  kg, and  $P < 10$  W.
  - Need for micropropulsion.
  - Plasma microthrusters introduce an additional complexity in their analysis due to the **overlap of electrodynamic and gasdynamic scales**.



# Physical Processes in a micro-PPT



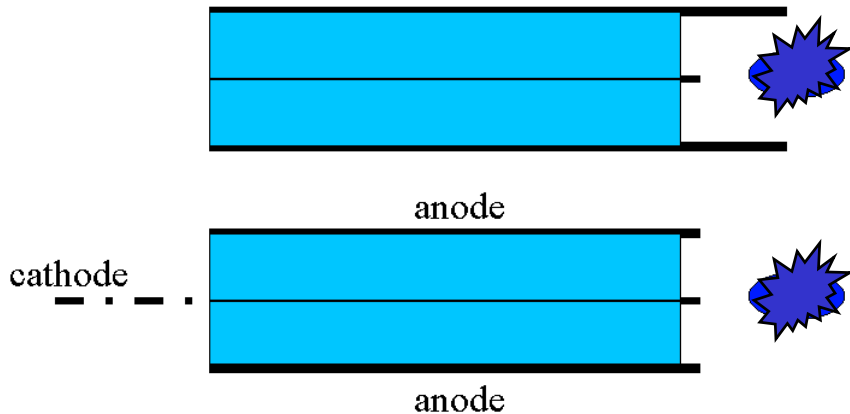
• Gas Discharge Processes

• Teflon Ablation

• Magnetogasdynamic Acceleration

• Coupling with External Circuit

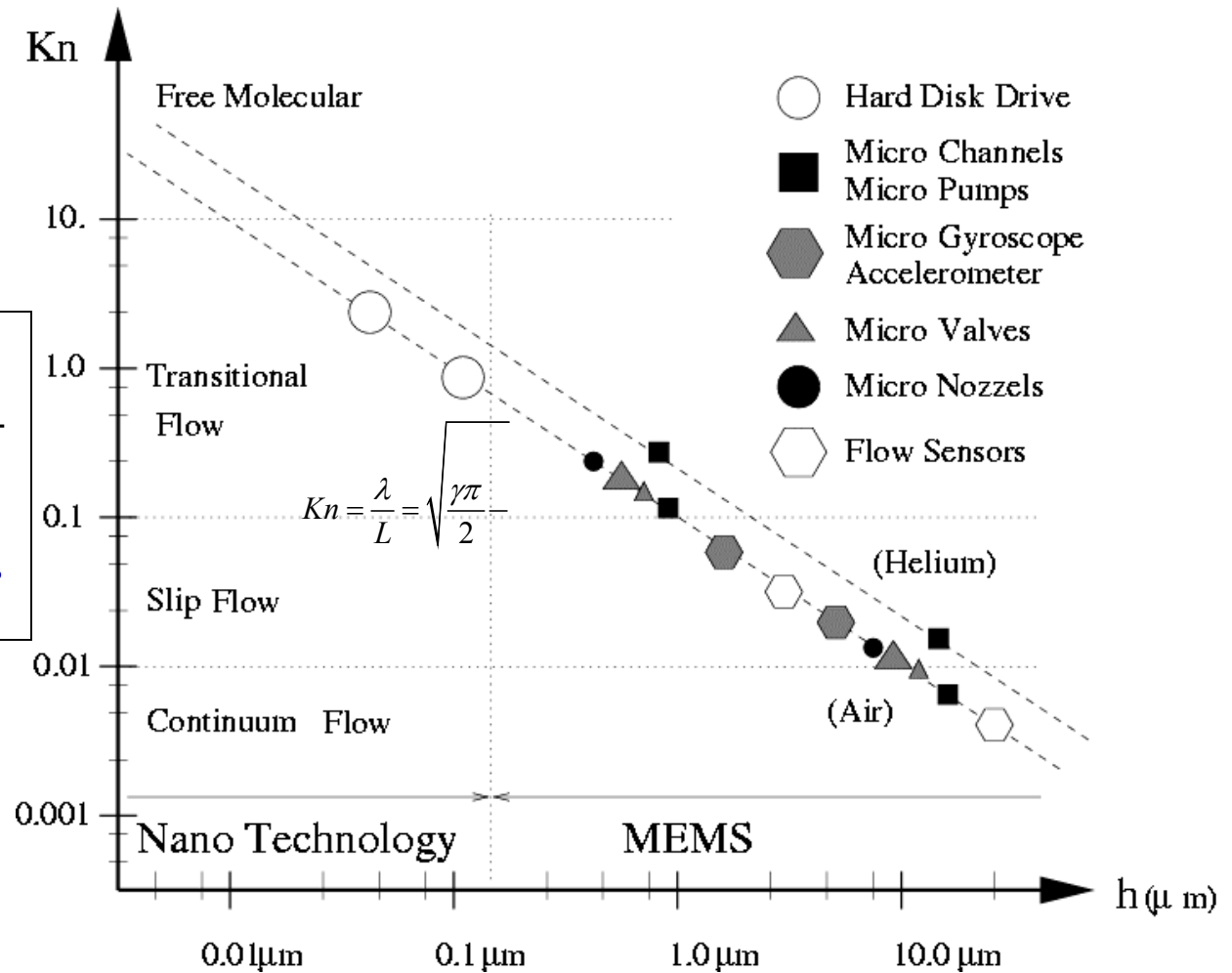
## AFRL micro-PPTs



# Gas Microflows: Typical Applications

$$Kn = \frac{\lambda}{L} = \sqrt{\frac{\gamma\pi}{2}} \frac{M}{Re}$$

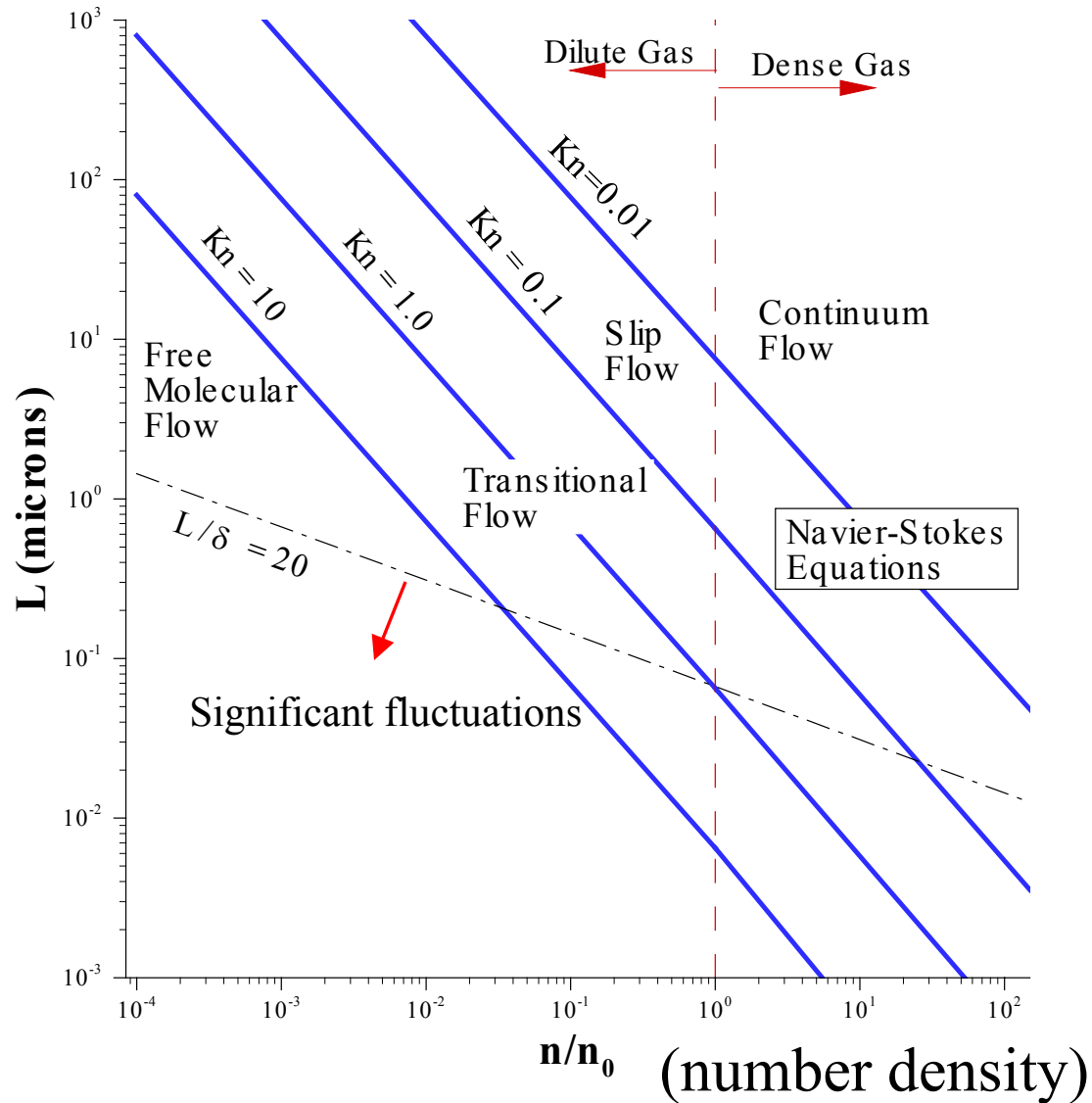
**Knudsen number**



# The Continuum Hypothesis

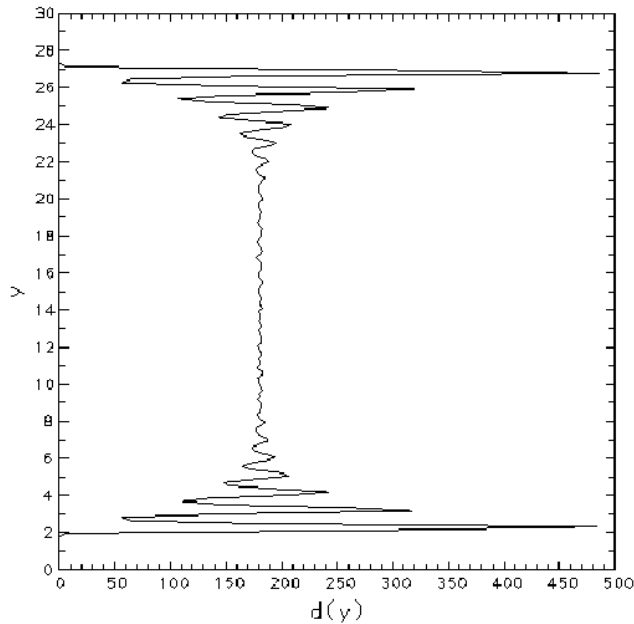
- How small should a volume of fluid be so that we can assign it *mean* properties?
- At what scales will the statistical fluctuations be significant?
- Are the low-pressure rarefied gas flows dynamically similar to the gas micro-flows?

# The Continuum Hypothesis

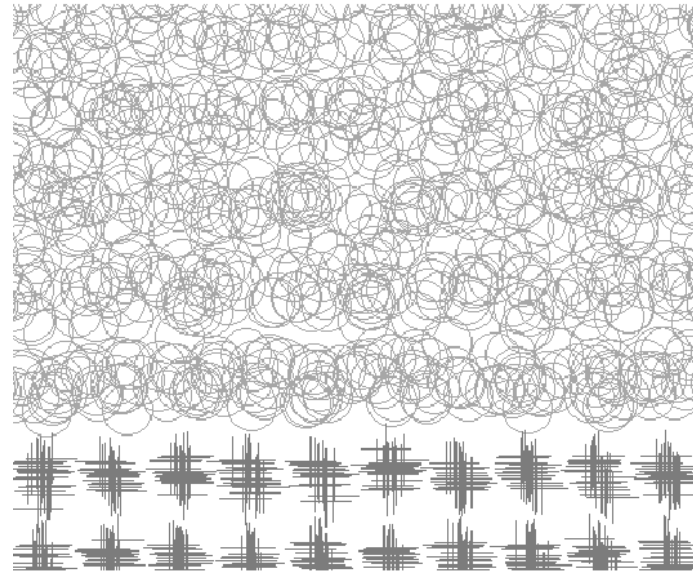


# LIQUIDS: Nano-Scale Behavior

## MD Simulations (*Koplik & Banavar, ARFM 1995*)



Density fluctuations across a nano-channel.



fluid

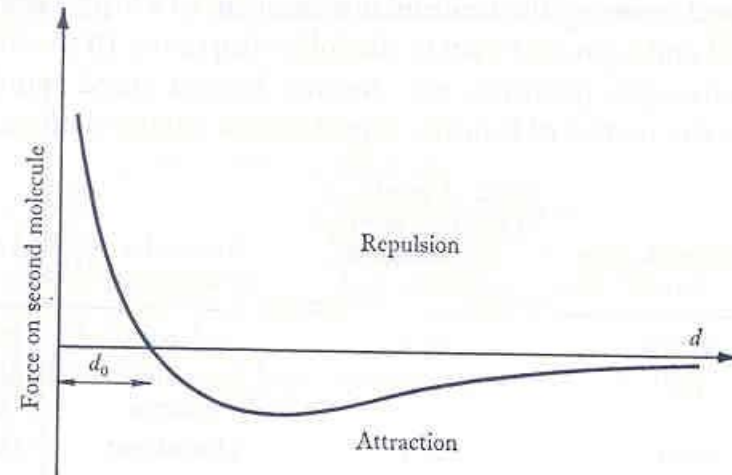
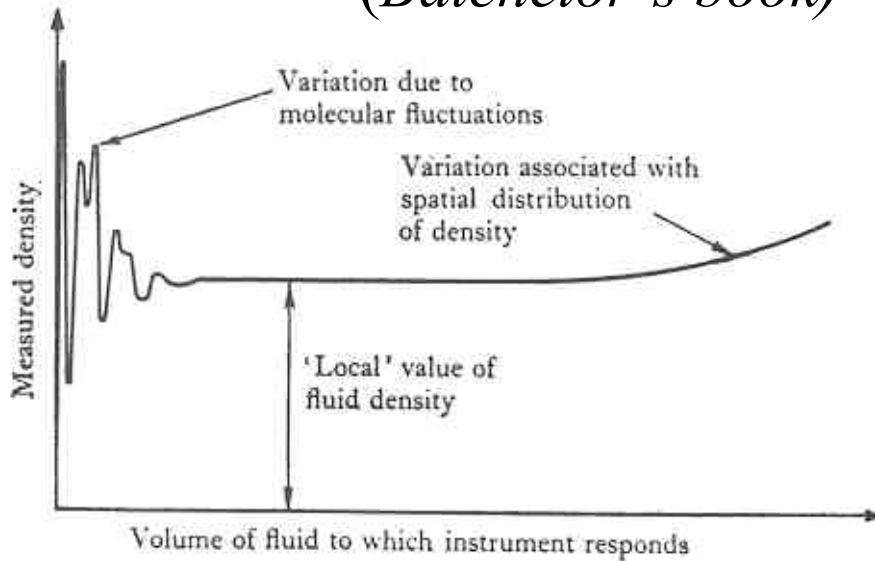
wall

Layering of Lennard-Jones molecules near a smooth surface.

- *3D periodic channel 51.30x29.7x25.65 (molecular units)*
- *27,000 number of atoms*
- *2,592 atoms of each wall (FCC lattice type)*
- *1 atom = 1 unit*

# The Continuum Hypothesis

•(*Batchelor's book*)

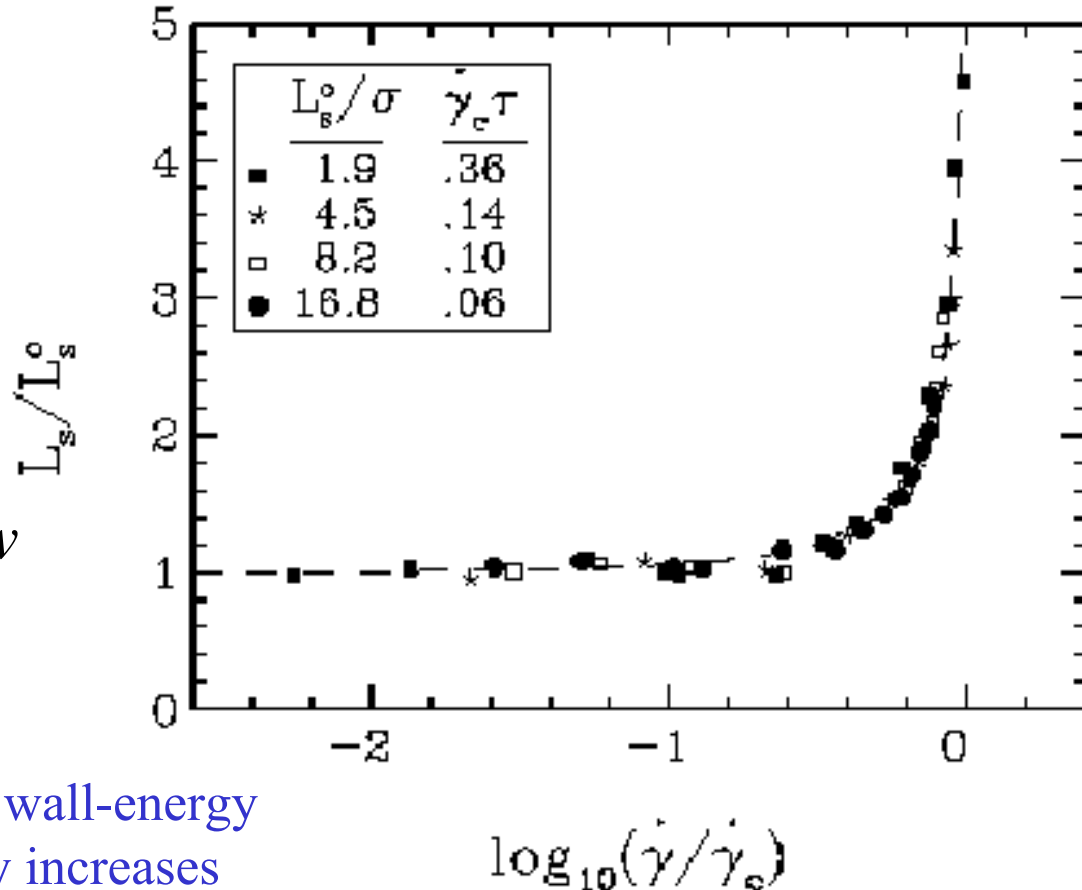


Type	Force (molec)	Motion ( $d_0$ )	Structure (molec)	statistics
Solid	Strong	$\ll 1$	ordered	quantum
Liquid	Medium	$O(1)$	Semi-order	quantum+ classical
gas	weak	$\gg 1$	disordered	classical

# Slip Length in Complex Liquids

(Thompson & Troian, *Nature*, 1998)

$$\frac{L_s}{L_s^0} = \left[1 - \frac{\dot{\gamma}}{\dot{\gamma}_c}\right]^\alpha$$



- MD of Couette flow
- Lennard-Jones
- $H=25.57\sigma$

- Slip length increases as wall-energy decreases or wall-density increases
- For slip length  $> 17\sigma$ :  
*strong nonlinear response?*

**Question: At high shear rates, is the liquid behavior near the wall non-Newtonian?**

# Physical Challenges of Micro-Scale Transport

- *Gas Flows*

- Compressibility
- *Rarefaction*
  - Slip
  - Transition
  - Free Molecular
  - Thermally Induced Motion
- Surface & Roughness
- Viscous Heating
- Incomplete Similitude
- ...

- *Liquid Flows*

- Wetting
- Adsorption
- Slip
- *Electrokinetics*
- Polarity
- Coulomb & van der Waals Forces
- Capillary Forces
- Roughness
- ...

**Constitutive Laws,  
Boundary Conditions,  
Surface, Interface and  
Body Forces**



## Numerical Modeling Challenges

- Multi Physical Phenomenon (Thermal, Fluidic, Mechanical, Biological, Chemical, Electrical)
- Multi Scale (Atomistic, Continuum)
- Complex Geometry

## Numerical Simulation Strategies

### ▶ Scientific Simulations:

- Multi Scale
- Simpler Geometry
- Accurate (error < 1 %)

### ▶ Engineering Simulations:

- Multi Scale
- Multi Physics
- Complex Geometry
- Accurate (error < 5~10 %)

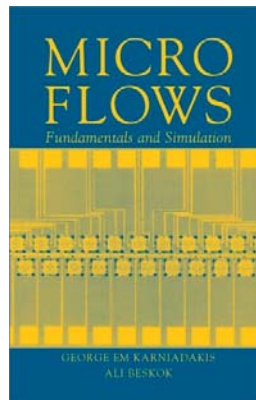
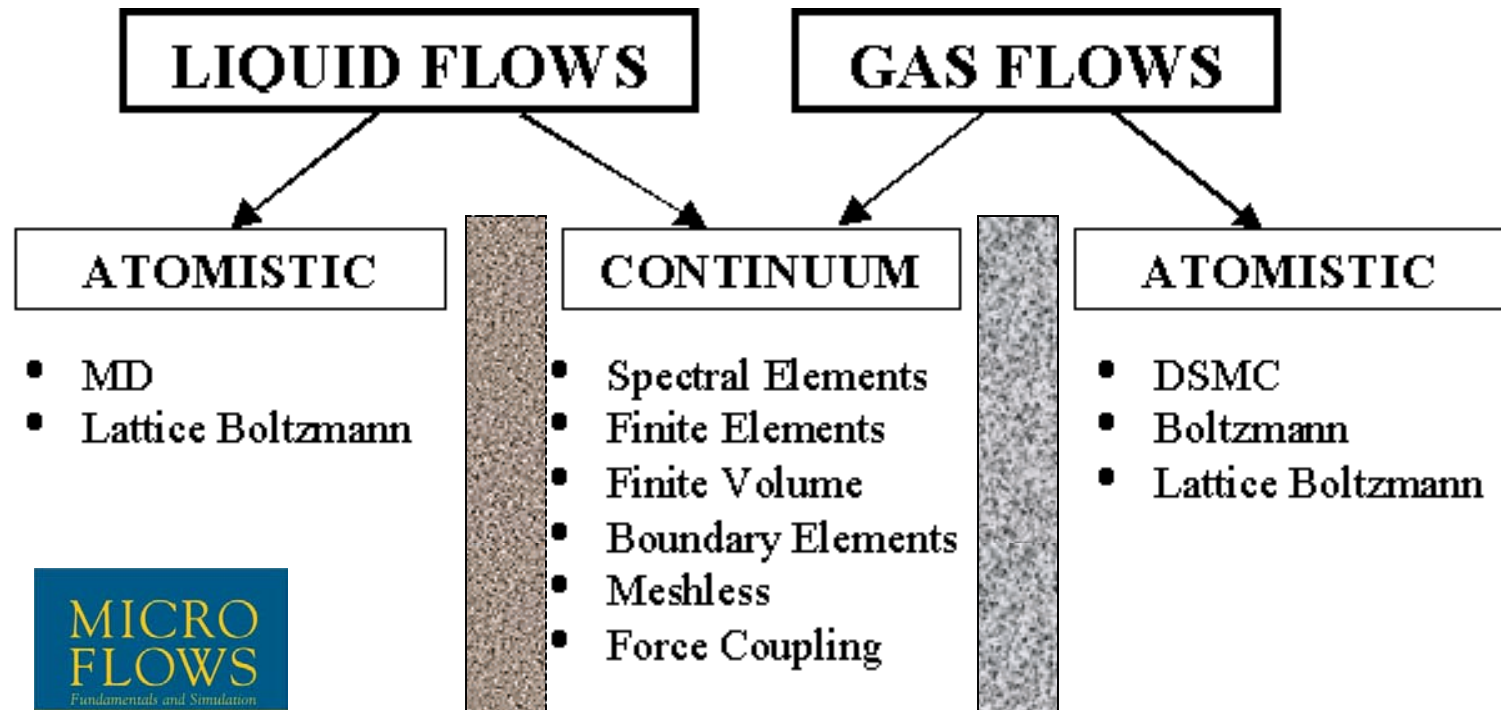
### ▶ Low Order Models:

- Multi Physics
- Full Device Simulation
- Lower Accuracy, but Fast (error ~10 %)

# *Challenges of Microscale Research*

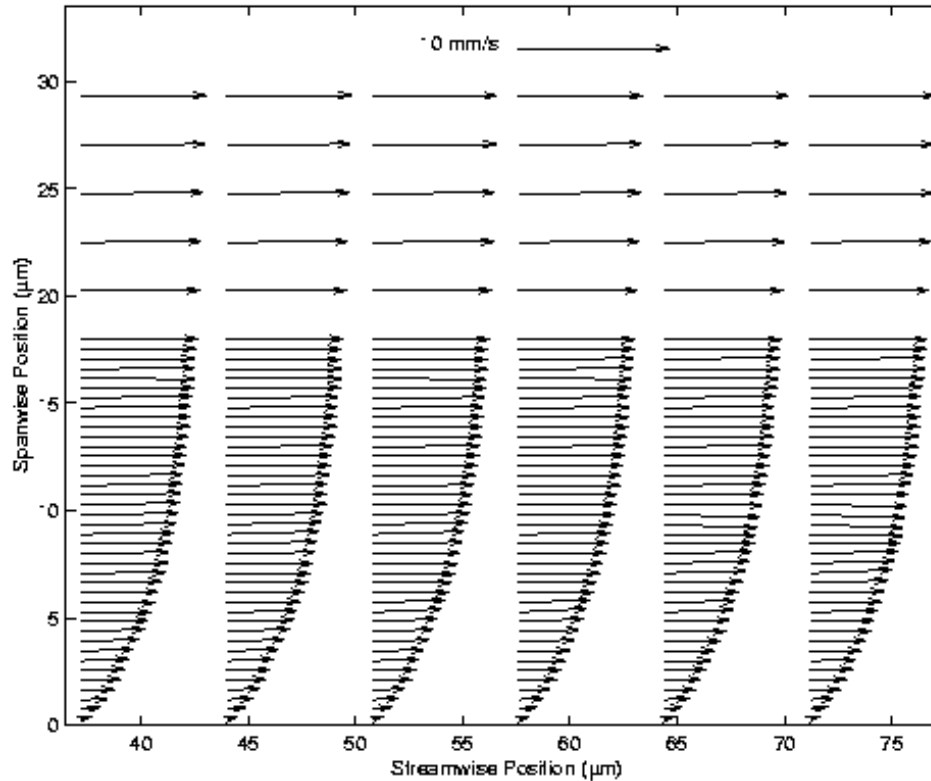
- **Small Scale Physics**
  - **Governing Equations Breakdown**
    - **Constitutive Laws**
    - **Boundary Conditions**
  - **Microscopic Effects**
    - **Dominance of Surface Forces**
    - **Coulomb Forces**
    - **Van der Waals Forces**
    - **Capillary Forces**
    - **Importance of Molecular Structure**
- **Detection & Experimental Verification**
  - **Micro Particle Image Velocimetry**
  - **Molecular Fluorescence Velocimetry**

# Numerical Modeling Methods



# Experimental Limitations

- Micro-Particle-Image-Velocimetry (*Meinhart et al.*)



- 30 x 300 microns channel
- Resolution: 450 nm in the wall-normal
- Overlapped windows
- Specialised interrogation algorithms

# Prototype Flows

- Pressure-Driven Flows
  - Poiseuille flow
- Shear-Driven Flows
  - Couette flow
  - Cavity flow
- Squeezed Film – Lubrication
  - Reynolds equation
- Electrokinetically-Driven Flows
  - Dielectrophoresis
- Thermal Creep
  - Knudsen compressors
- Surface-Tension-Driven Flows
  - routing of droplets

# FUTURE

- Microfluidics:

The path and link to nanotechnology

- The wet circuit → liquid circuit + element

- Fluidic Self Assembly – Massively Parallel VLSI-like, programmable fluidic networks with logic

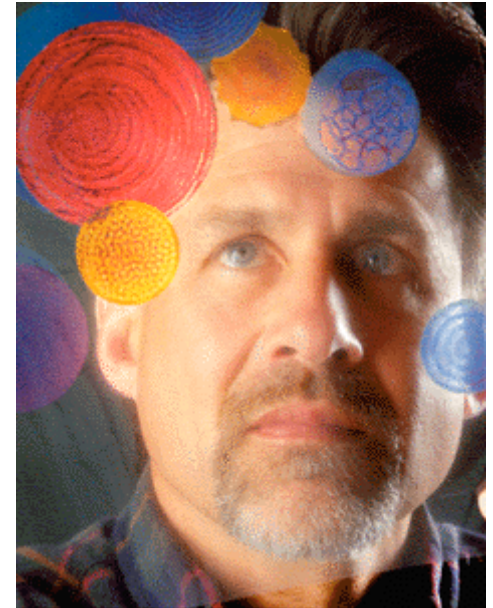
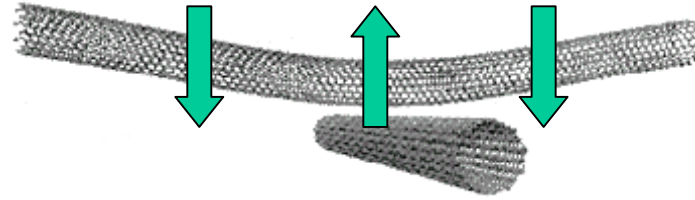
- Fluids with more than Viscosity – MOEMS

- Complex Fluids

- Magnetorheological fluids
- Magnetic (high-frequency) microfluidics
- Dynamic reconfiguration, use **E** to change properties

- Wall-less fluidics/interfaces (Bebe, Whitesides)

- Smart dust – Biomimetic sensors



*Sandia nanospheres*

