Electron-phonon coupling and the zero-point phonon renormalization of the electronic band gap

Michel Côté¹

¹Université de Montréal

The coupling of electrons to a bosonic field generally causes a renormalization of the energy levels. Whereas in vacuum, the electromagnetic fluctuations lead to the Lamb shift observed in the hydrogen atom levels, in condensed matter, the phonon field renormalizes the band structure, even at zero temperature. Being as large as several hundreds of meV, this renormalization is critical to the predictive power of ab initio calculations when it comes to absorption spectra, photovoltaic materials, or topological insulators. Following the early work of Fan and others in the 1950s, the problem was addressed by Allen, Heine and Cardona, whose theory provides perturbative expressions in terms of the electron-phonon coupling. Using semi-empirical methods, and later on, density functional theory (DFT), the temperature dependence of the band gap could be obtained for several semiconductors. Among those, diamond has become a case study where the zero-point renormalization is as much as half an election volt. The reliability of DFT for the electron-phonon coupling has however been challenged in recent years. Since the scattering of an electron by a phonon probes the excited states of a system, a theory describing this process should rely on an accurate unrenormalized band structure, unlike the one of DFT. A truly ab initio scheme however would rely on many-body perturbation theory. In this presentation, I will report on how a careful treatment using manybody perturbation theory as implemented by the GW approach result in an enhancement of the electron-electron interaction causing a 40% enhancement in the zero-point renormalization (ZPR) in diamond with respect to the usual DFT treatment.