

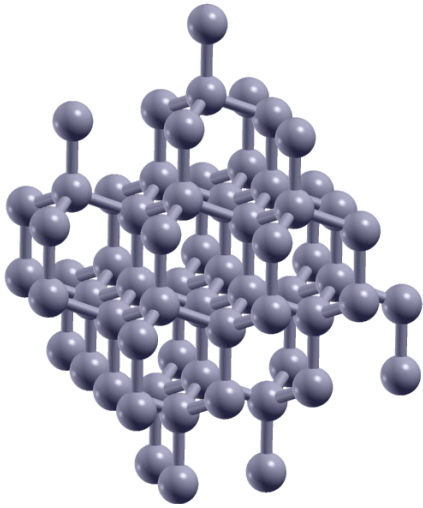
# Superconductivity and Magnetism in Amorphous Carbon

Yuki Sakai

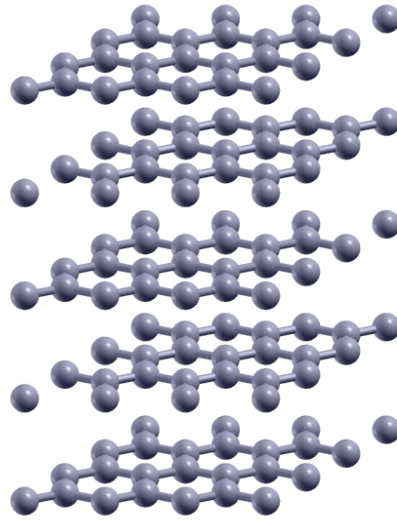
Oden Institute for Computational Engineering and Sciences,  
The University of Texas at Austin

2019 Electronic Structure Workshop  
May 22, 2019

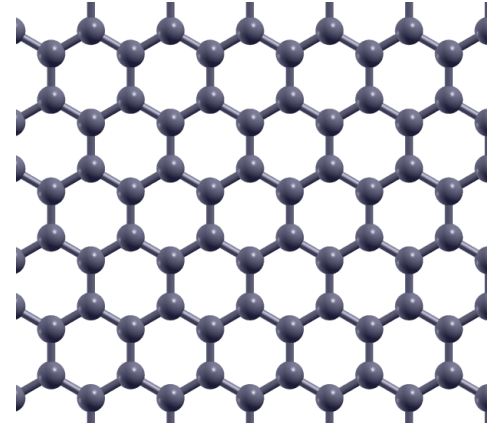
# Allotropes of carbon



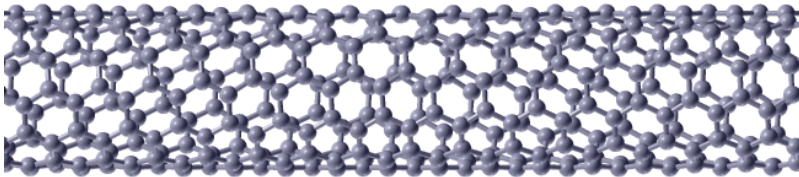
Diamond



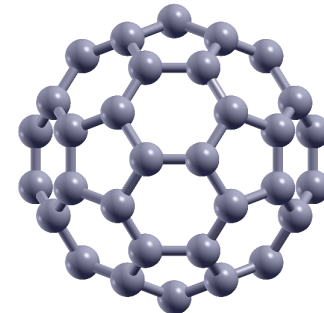
Graphite



Graphene



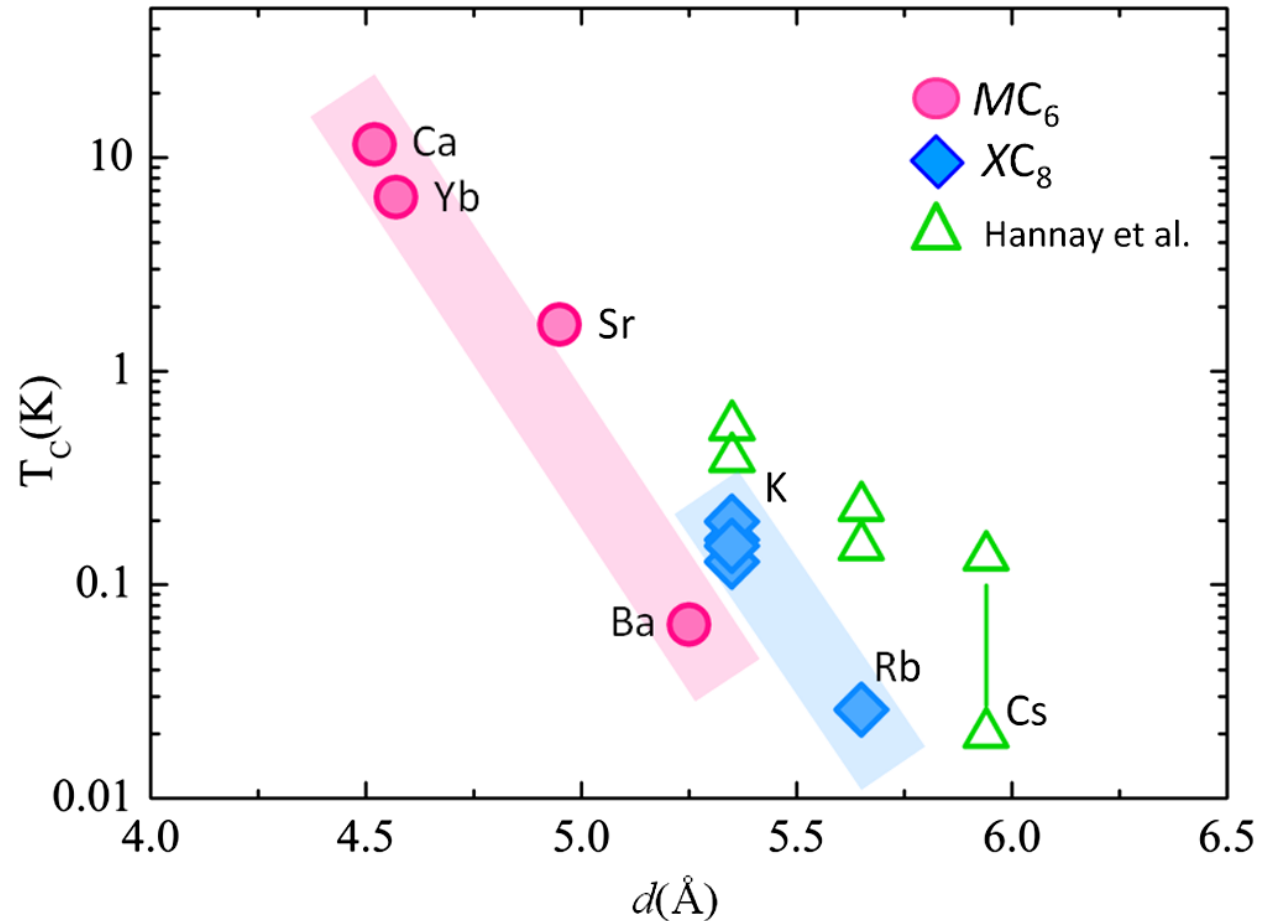
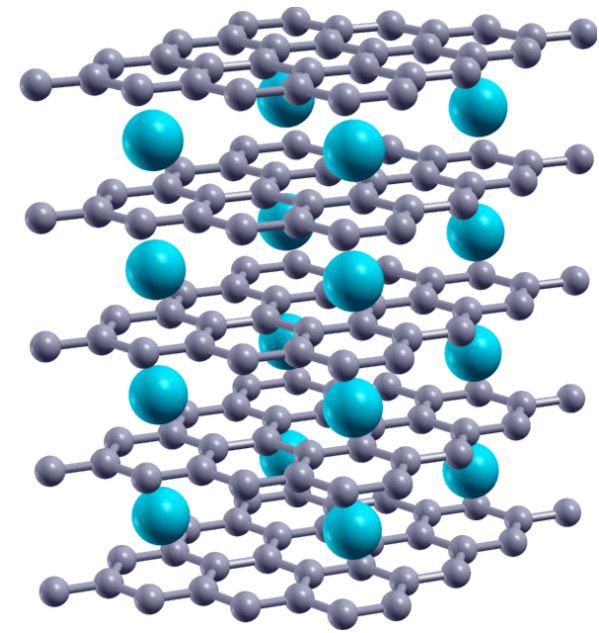
Carbon nanotubes



Fullerene

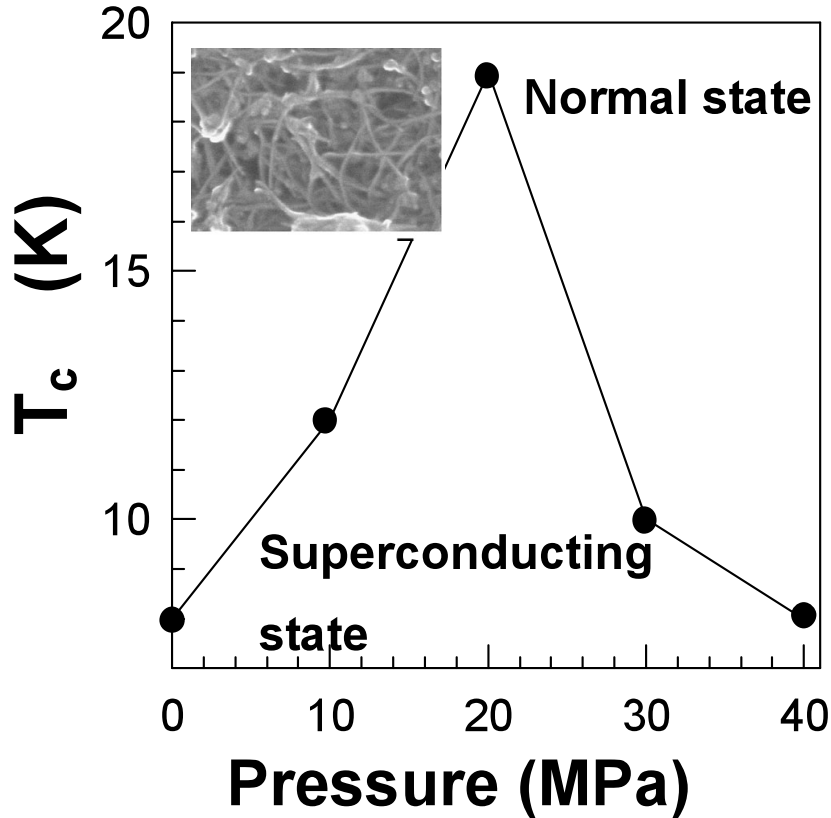
Various physical properties associated with various structures

# Superconductivity in carbon materials

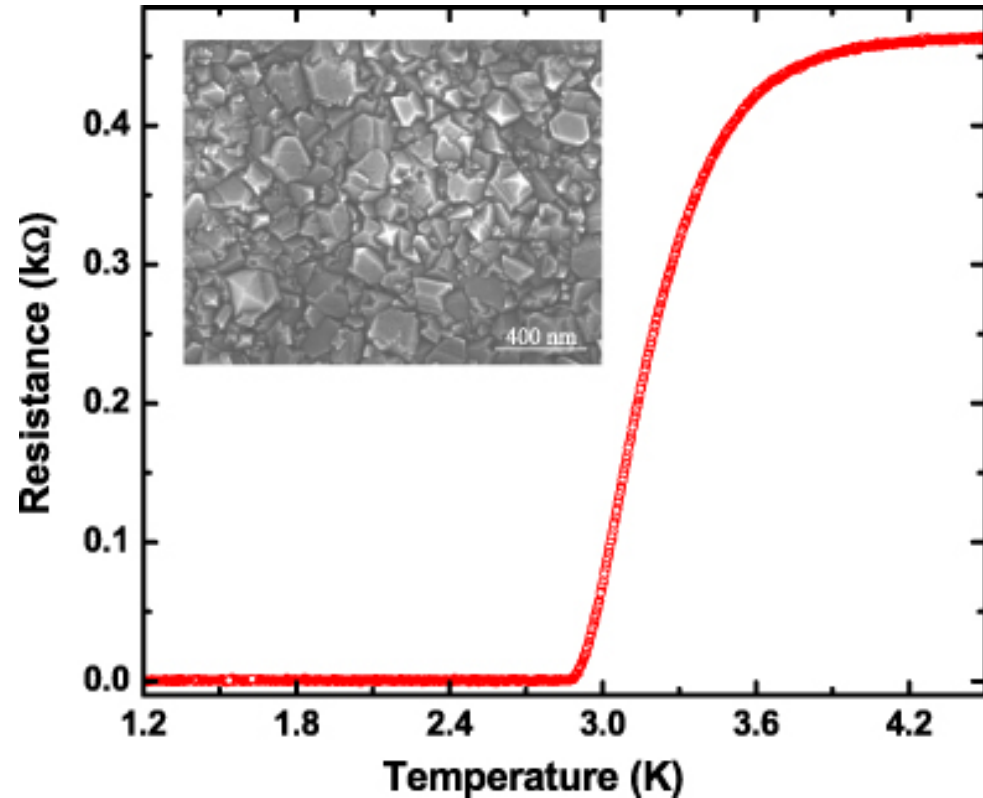


Graphite Intercalation Compounds  
(Electron doping from intercalants)

# Superconductivity in B-doped carbon



B-doped carbon nanotubes

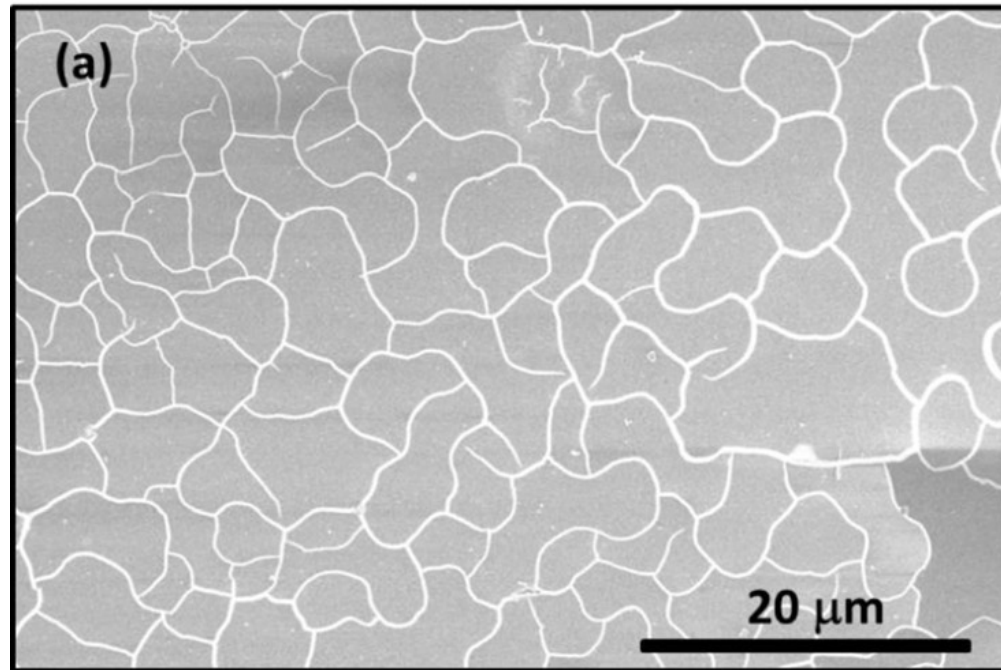


B-doped diamond

Can be superconductors when substitutionally boron doped



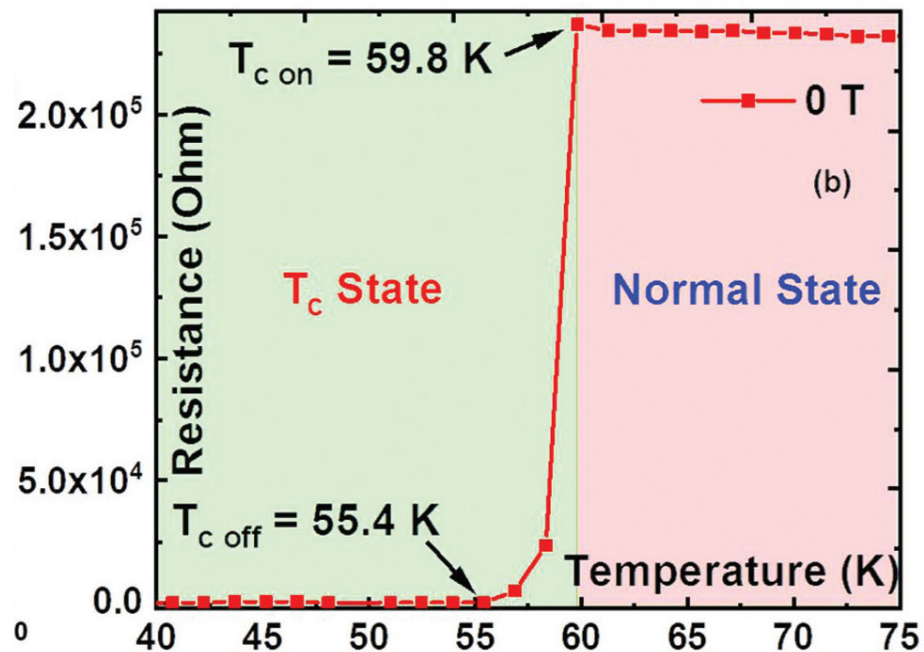
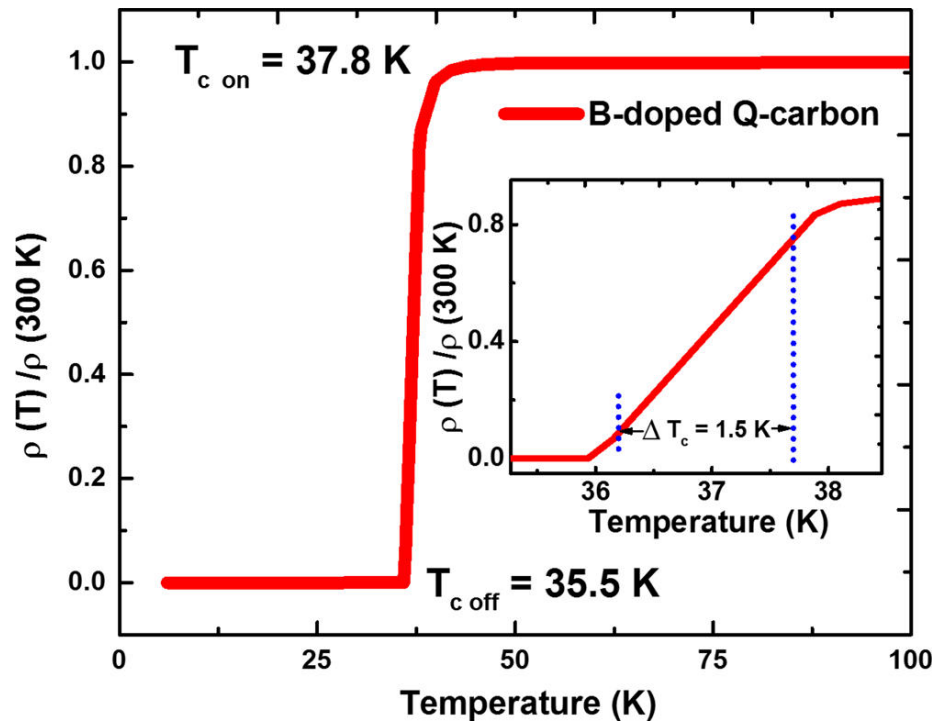
# New amorphous carbon: Q-carbon



Scanning electron microscopy image

New form of amorphous carbon with 75-85 % of  $sp^3$ -hybridized carbon atoms

# Superconductivity in B-doped Q-carbon



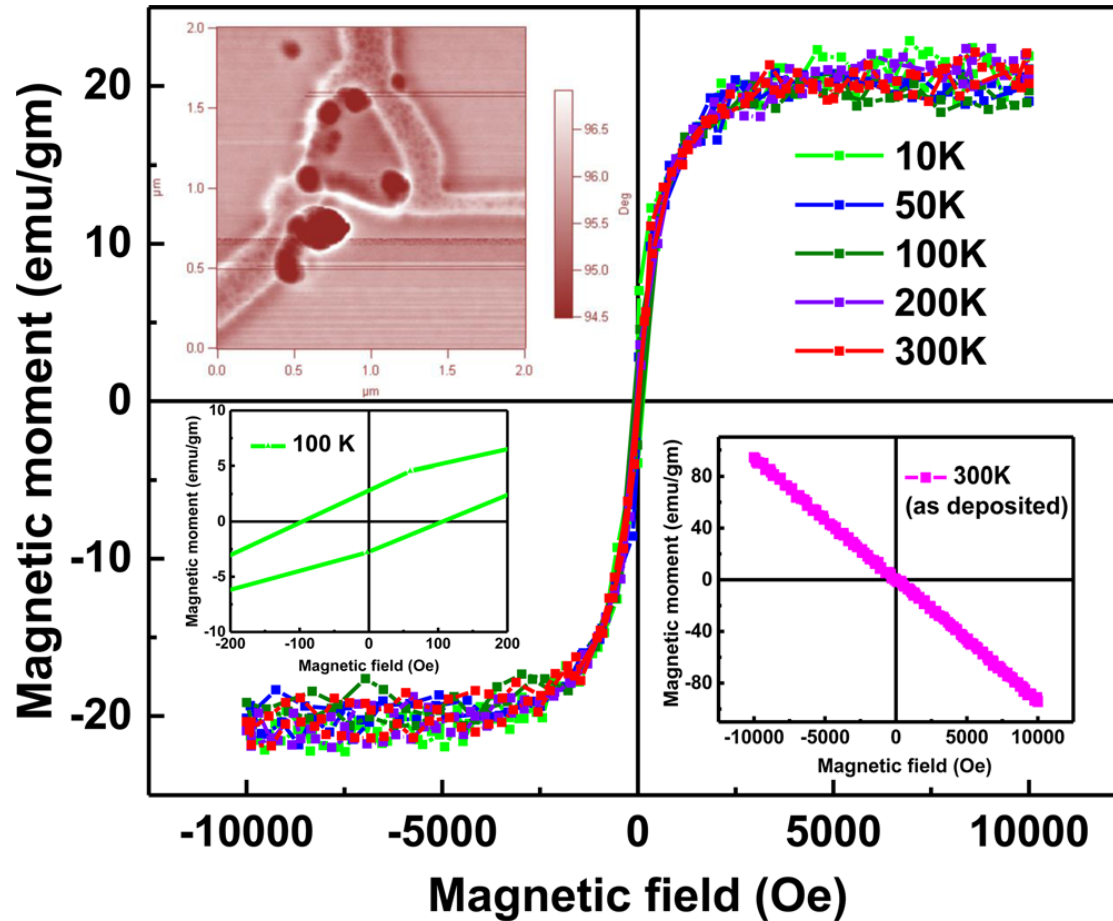
## Temperature dependence of resistivity

- $T_c$  of 36 (55) K when 17 (27) % boron doped
- Higher than  $T_c$  of B-doped diamond (11 K) or nanotubes (19 K)
- Highest  $T_c$  in carbon materials

A. Bhaumik, et al., ACS Nano **11**, 5351 (2017).

A. Bhaumik and J. Narayan, Nanoscale (2019)

# Magnetic properties of Q-carbon

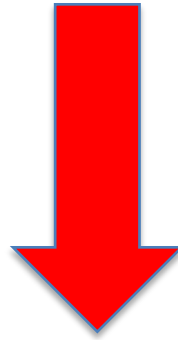


Ferromagnetism ( $0.4 \mu_B/\text{atom}$ ) at room temperature unusual in carbon materials

# Purpose of research

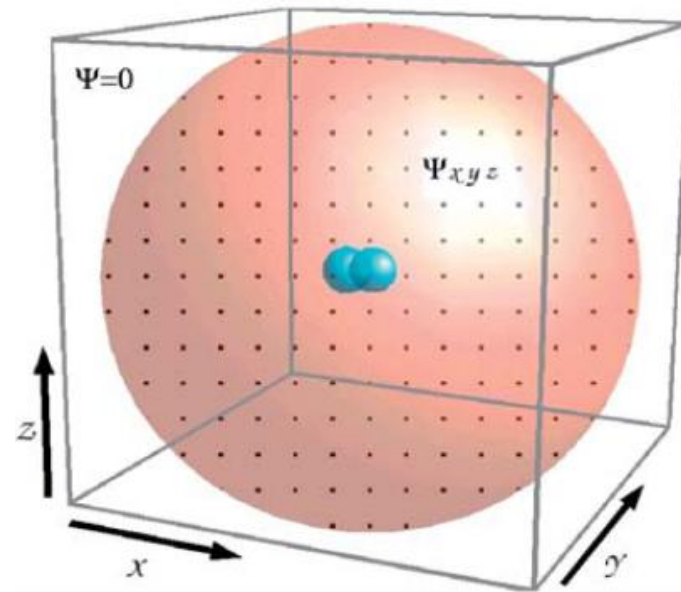
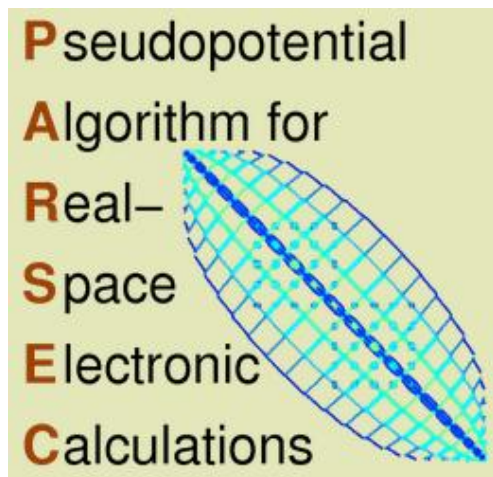
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Investigate magnetism and  
superconductivity in amorphous carbon



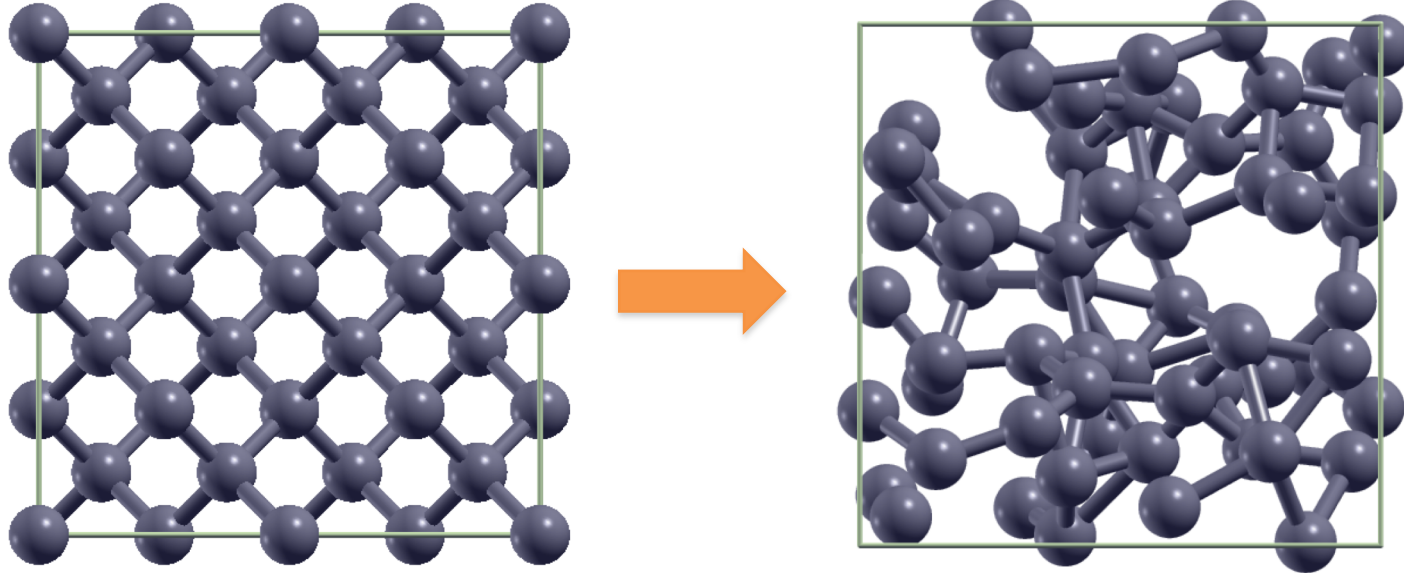
Understand interesting physical properties of Q-carbon  
(with unknown amorphous structure)

# Realspace pseudopotential DFT code PARSEC



- Solve Kohn-Sham equations on realspace grid points without explicit basis function
- Grid spacing as a convergence parameter
- Less global communication
- Applied to systems with  $\sim 20k$  atoms

# Generating amorphous structure

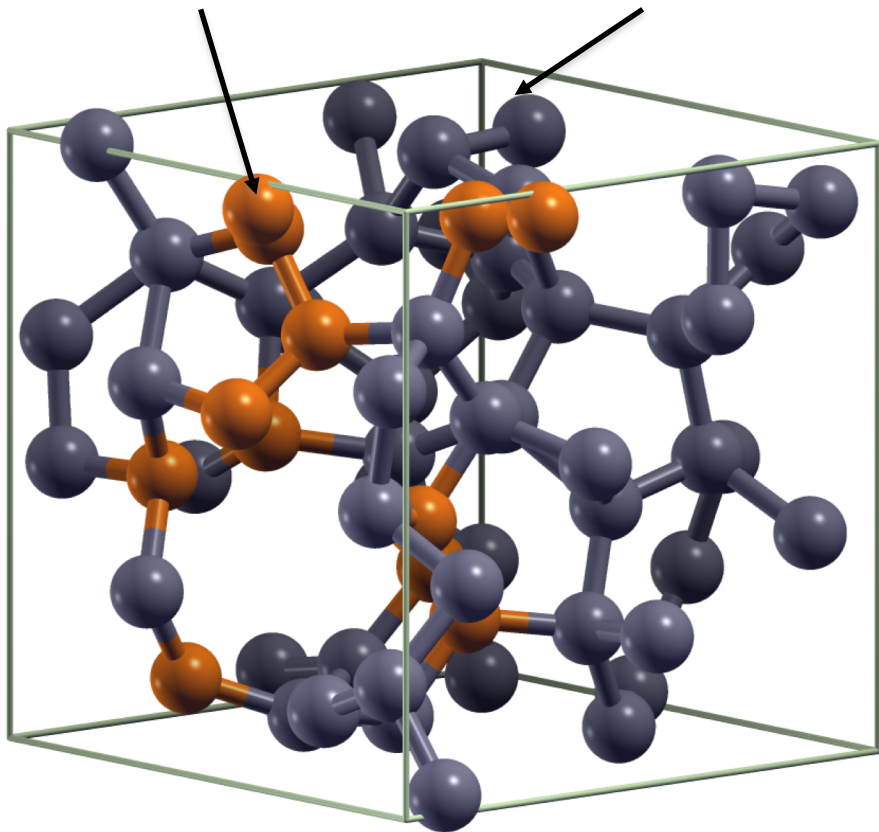


- Molecular dynamics simulation using PARSEC
  - Simulating melting process
- NVT ensemble molecular dynamics
  - Langevin thermostat
  - Obtain randomized (liquid-like) atomic coordinates
- Relax (quench) the structure

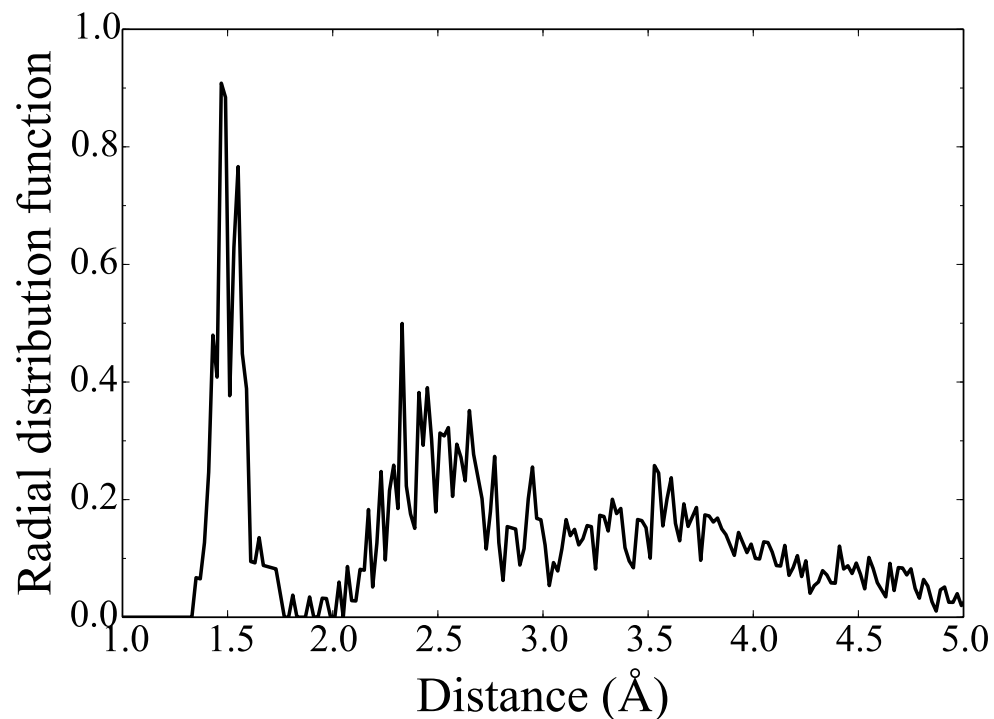
# Undoped amorphous carbon

$sp^2$

$sp^3$



Structure ( $3.4 \text{ g/cm}^3$ )



Radial distribution function



# Outline

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- Magnetism in amorphous carbon
- Superconductivity in B-doped amorphous carbon

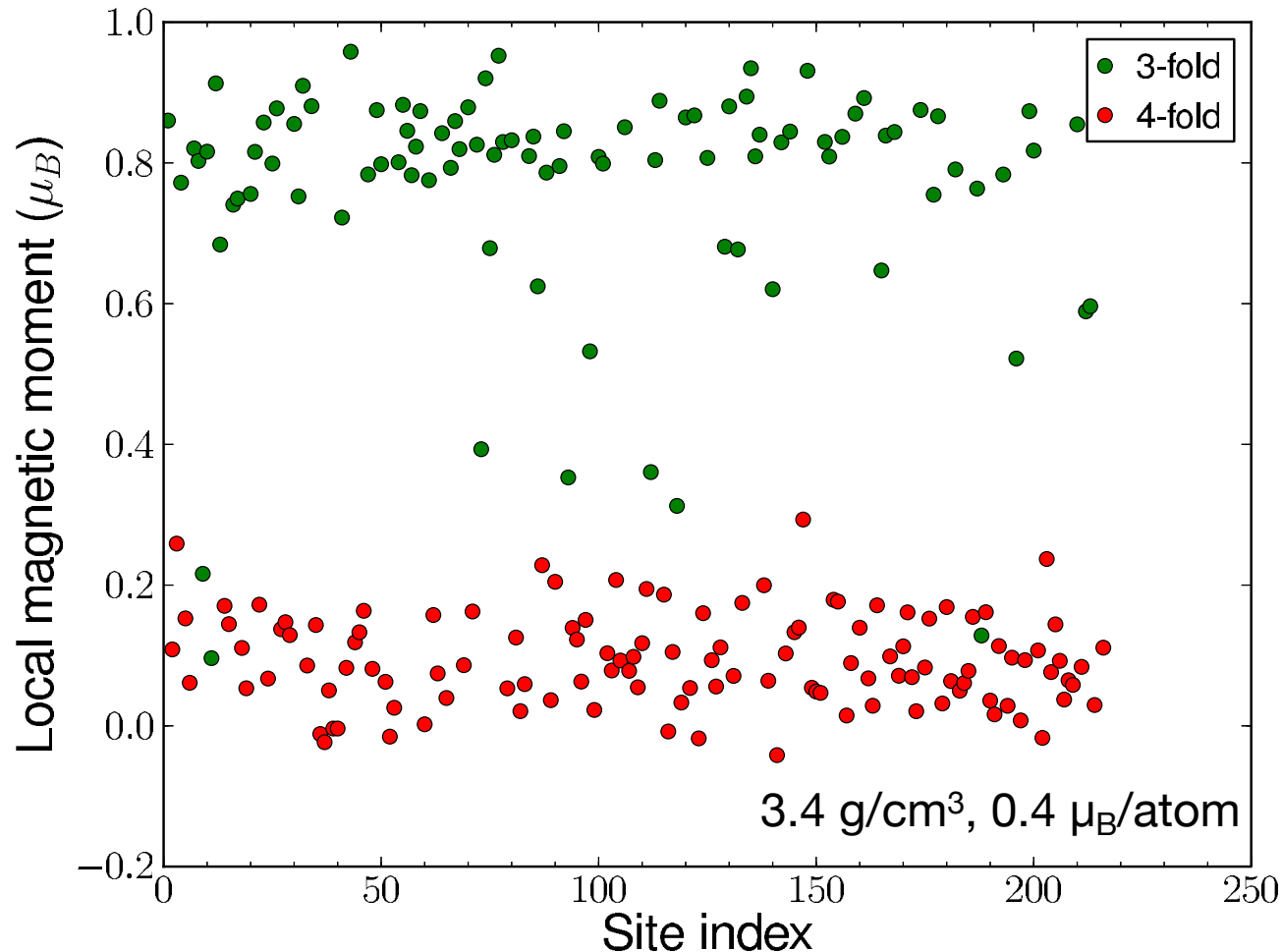
# Computational method (magnetism)

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- 216-atoms supercell
- Different mass densities from 2.6 to 3.4 g/cm<sup>3</sup>
- Optimize structure **under fixed magnetization** for the study of magnetism
  - Imposing two different Fermi energies for two orientations of electron spins
  - 0 to 0.4  $\mu_B$ /atom (experimental value)

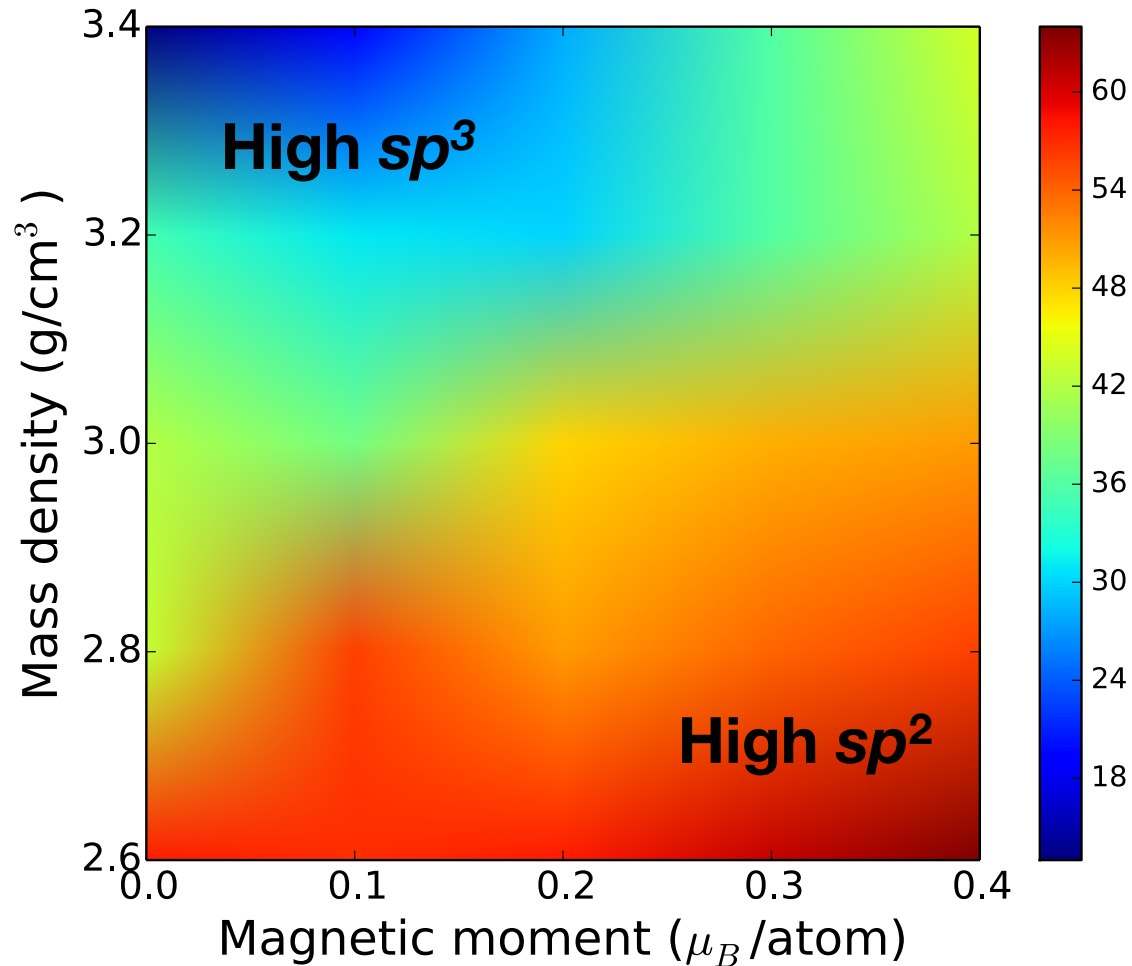
Study structural and energetic properties as a function of mass density and fixed magnetization

# Distribution of magnetic moments



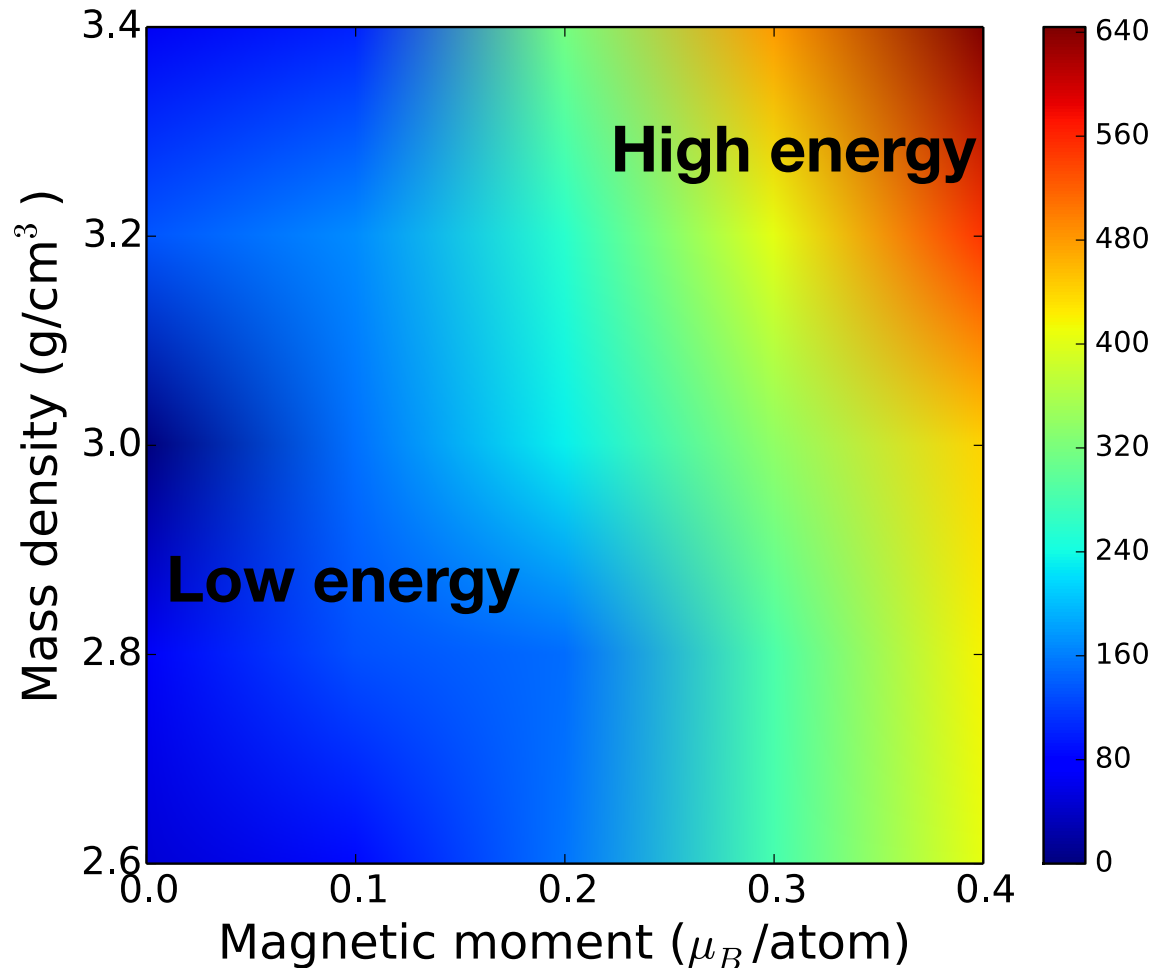
- Magnetic moments are mostly at  $sp^2$  hybridized (3-fold coordinated) carbon sites
- Unpaired electrons from  $sp^2$  hybridized atoms

# Proportion of $sp^2$ hybridized atoms



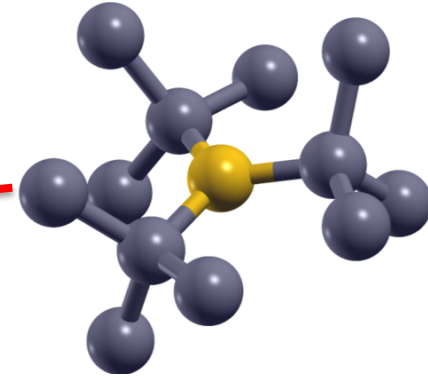
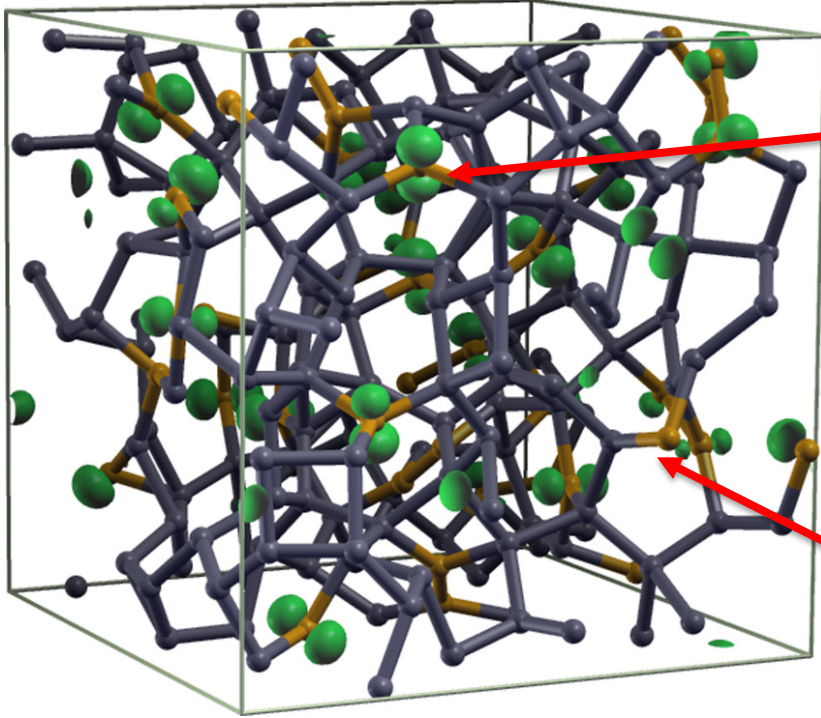
- High  $sp^3$  proportion in high density cases
- High  $sp^2$  ratio is necessary for high magnetization

# Total energy (meV/atom)

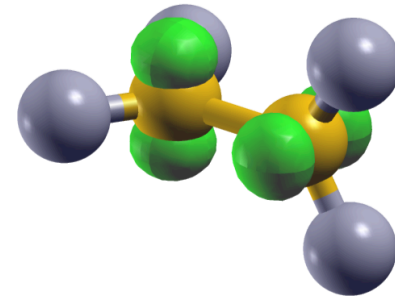


- High energy in structure with high magnetic moment
- Experimental magnetization (0.4 μ<sub>B</sub>/atom) yields high energy more than 400 meV/atom

# Two typical local geometries



$sp^2$  atom surrounded by  $sp^3$  atoms

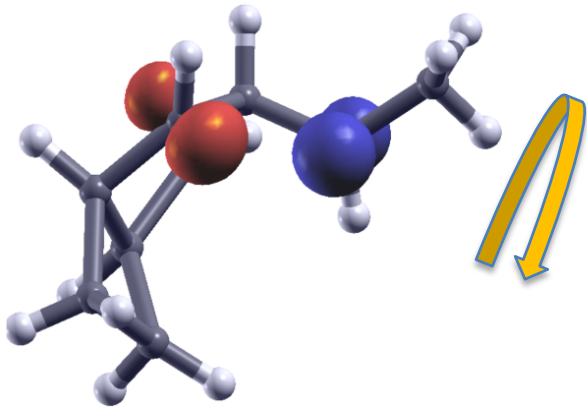


Two  $sp^2$  atoms bonded but rotated by  $90^\circ$

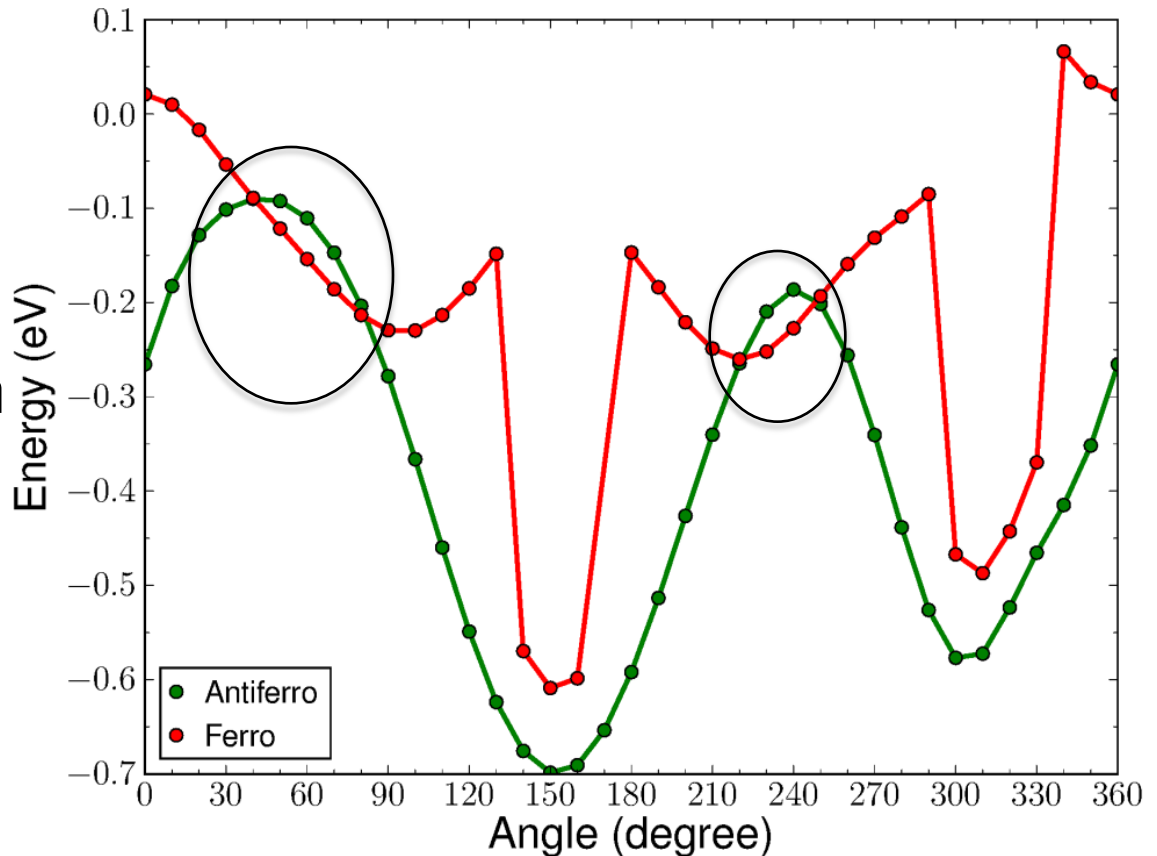
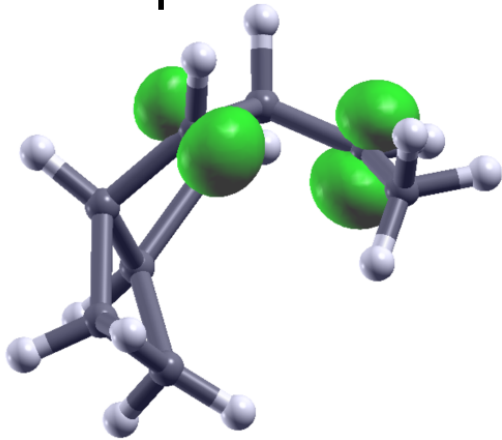
Spin charge density  
( $3.4 \text{ g/cm}^3$ ,  $0.1 \mu_B/\text{atom}$ )

- $0.05 \mu_B/\text{atom}$  remains after releasing constraint
- Magnetization is possible but smaller than experimental value

# Energy comparison in “molecule”



Artificial “molecule” from amorphous structure



- Total energy depends on the relative angle of  $p$  orbital
- Lower energy in the spin-parallel case



# Summary

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- Magnetism in amorphous carbon
  - Importance of  $sp^2$ -hybridized atoms
  - High energy in experimental magnetization
  - Small magnetization is possible
- Superconductivity in B-doped amorphous carbon

# Computational method (superconductivity)

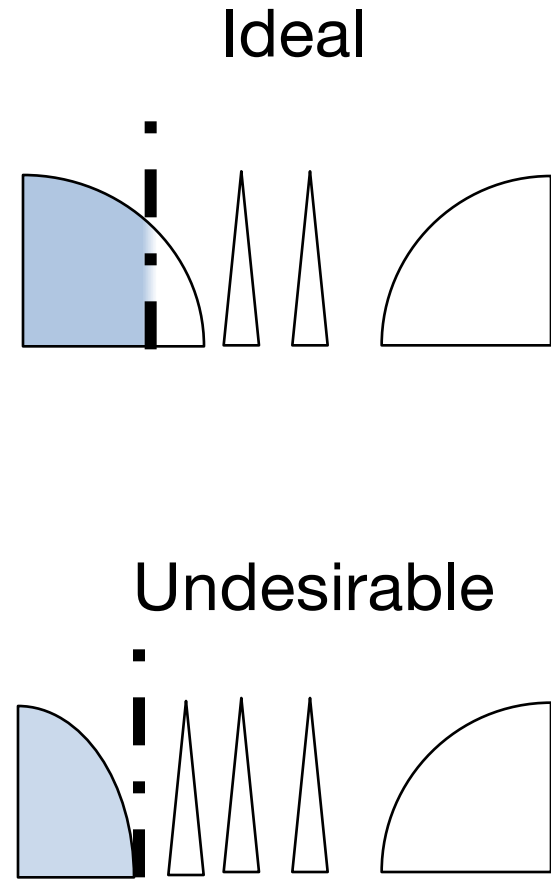
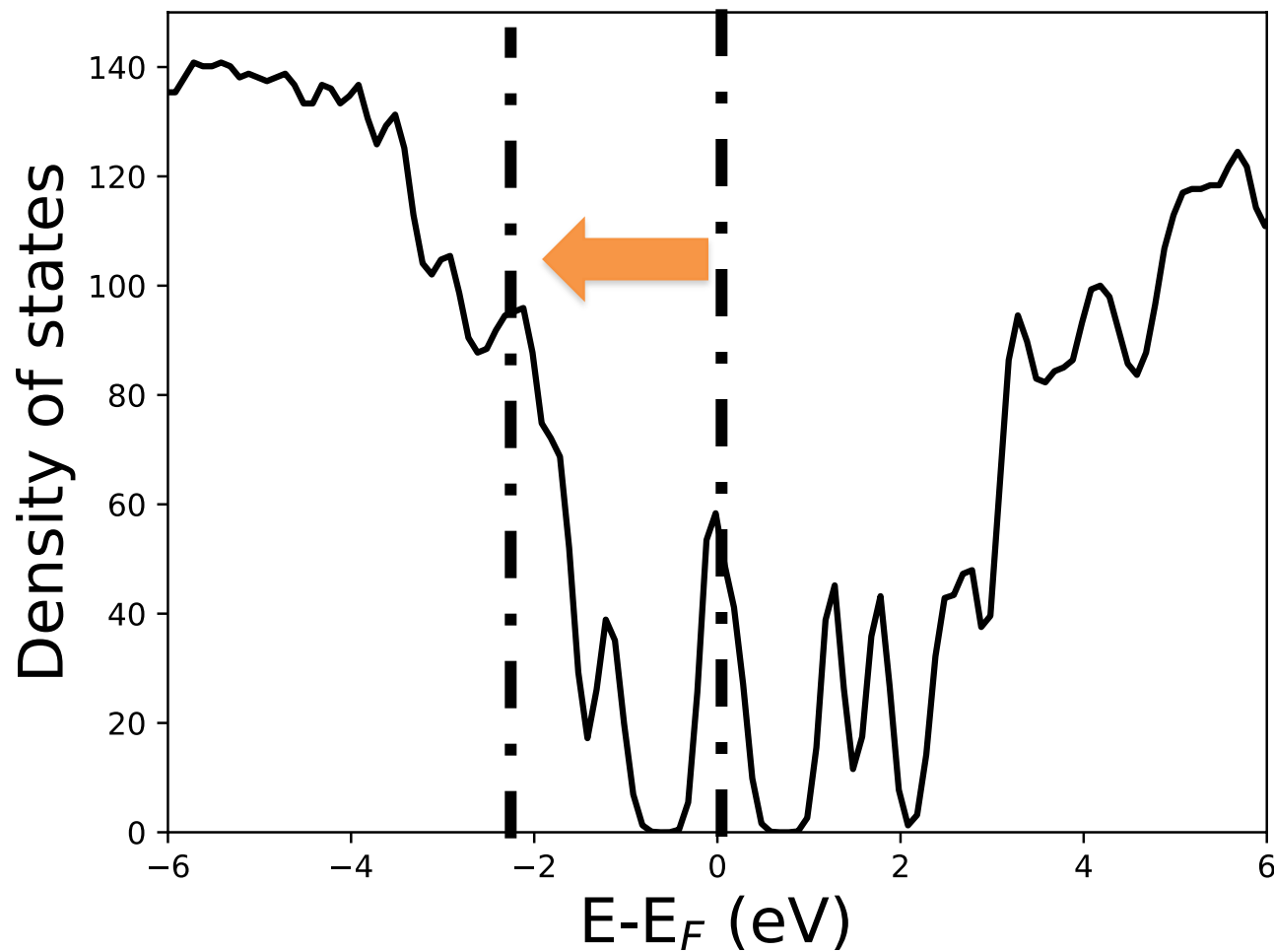
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- 64-atoms supercell
- Up to 12.5 % boron doping (8 of 64 atoms)
- Substitutional B doping **one by one**
- Density functional perturbation theory for phonon modes and electron-phonon coupling constant
- Allen-Dynes equation for  $T_c$  estimation ( $\mu^*$  of 0.12)

$$T_c = \frac{\omega_{\log}}{1.2} \exp \left[ \frac{-1.04(1 + \lambda)}{\lambda(1 - 0.62\mu^*) - \mu^*} \right]$$

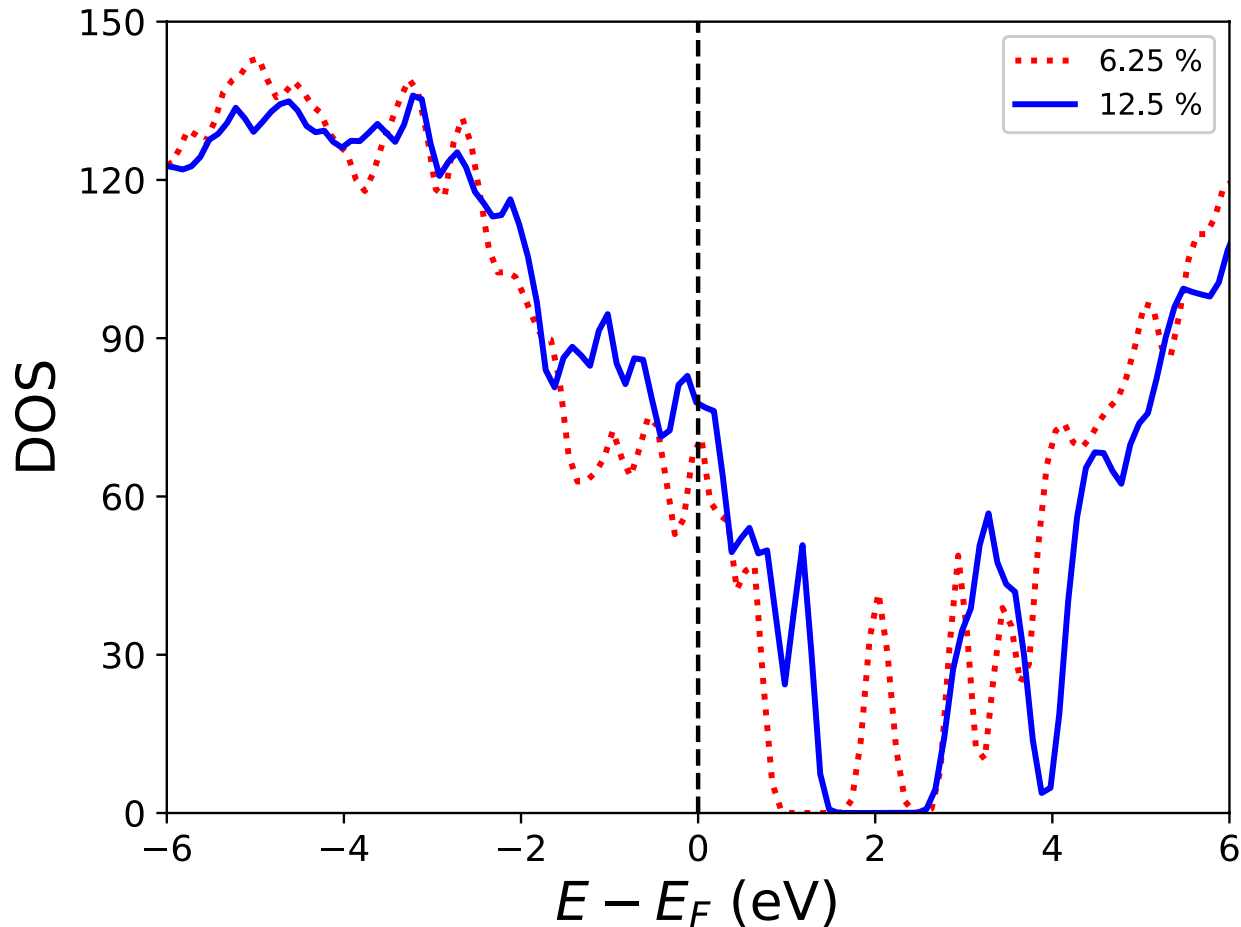


# Engineering electronic density of states



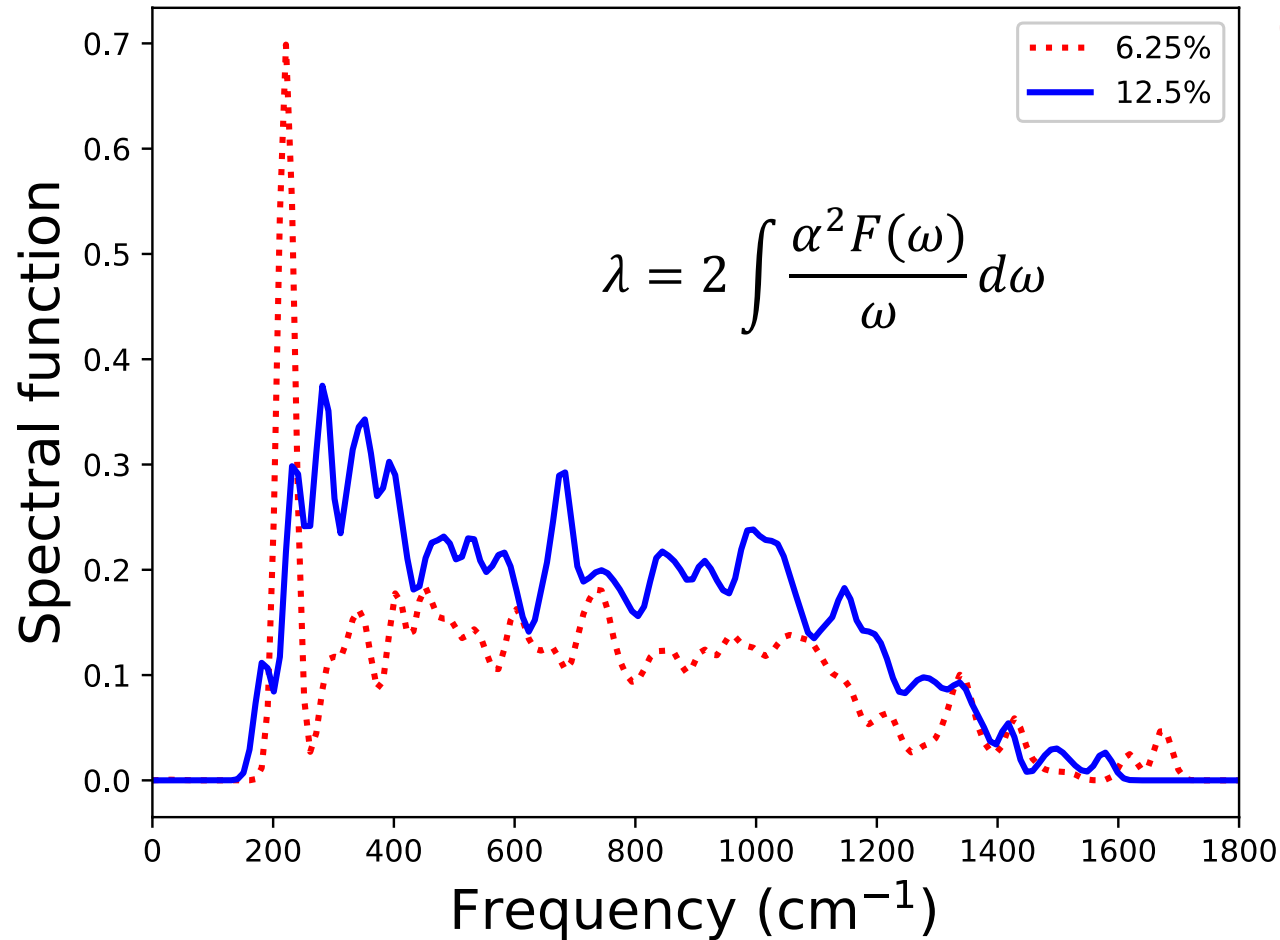
By doping boron atoms, shift the Fermi energy toward valence band without creating localized (deep) impurity states

# Evolution of electronic structure



- One by one substitutional B doping to avoid creating localized defect levels
- Choose substitutional site not by low total energy, but electronic properties

# Eliashberg spectral function



6.25 % doped

$$\lambda = 0.64$$

$$T_c = 13 \text{ K}$$

12.5 % doped

$$\lambda = 0.89$$

$$T_c = 34 \text{ K}$$

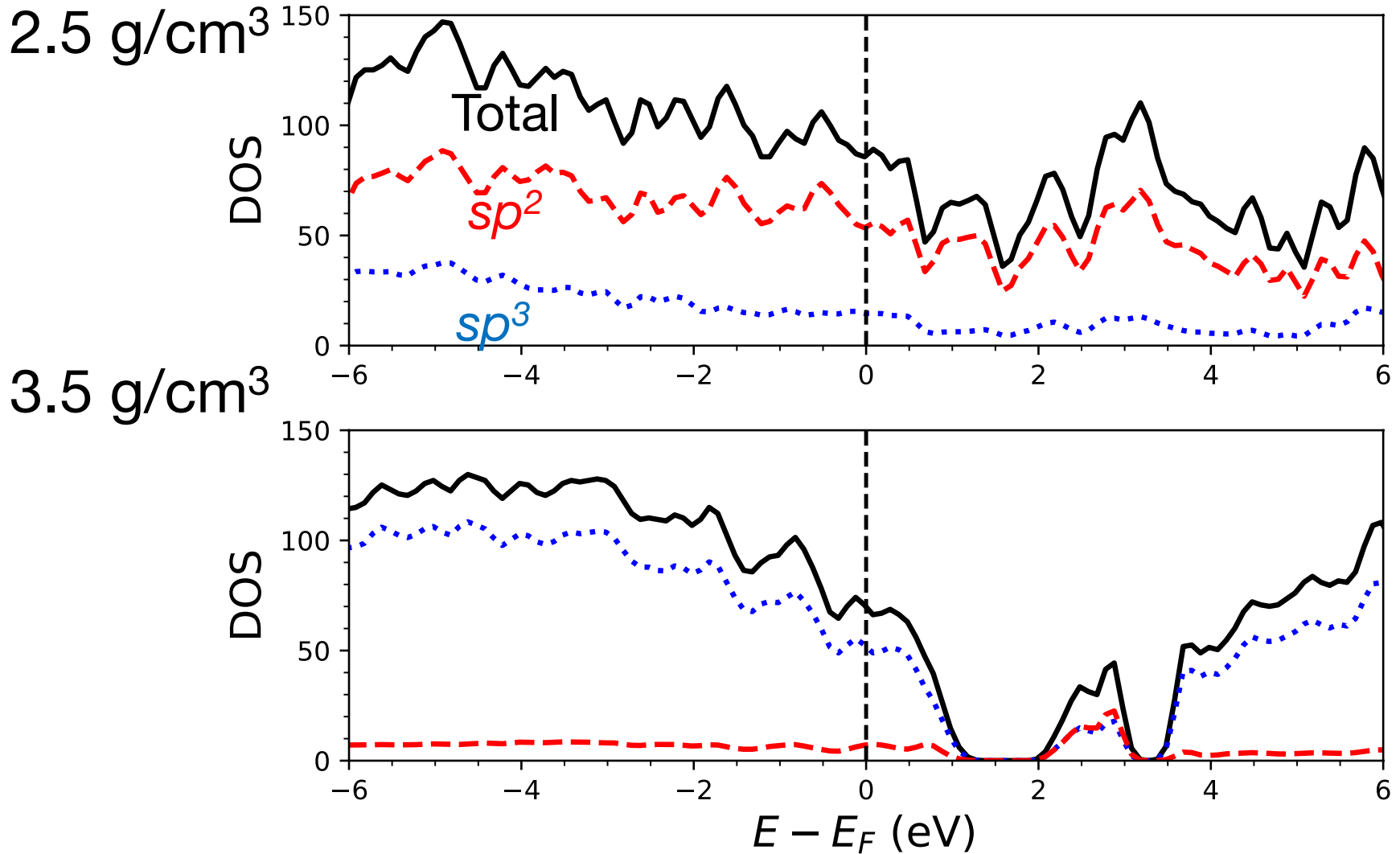
Experimental

17 % doped

$$T_c = 36 \text{ K}$$

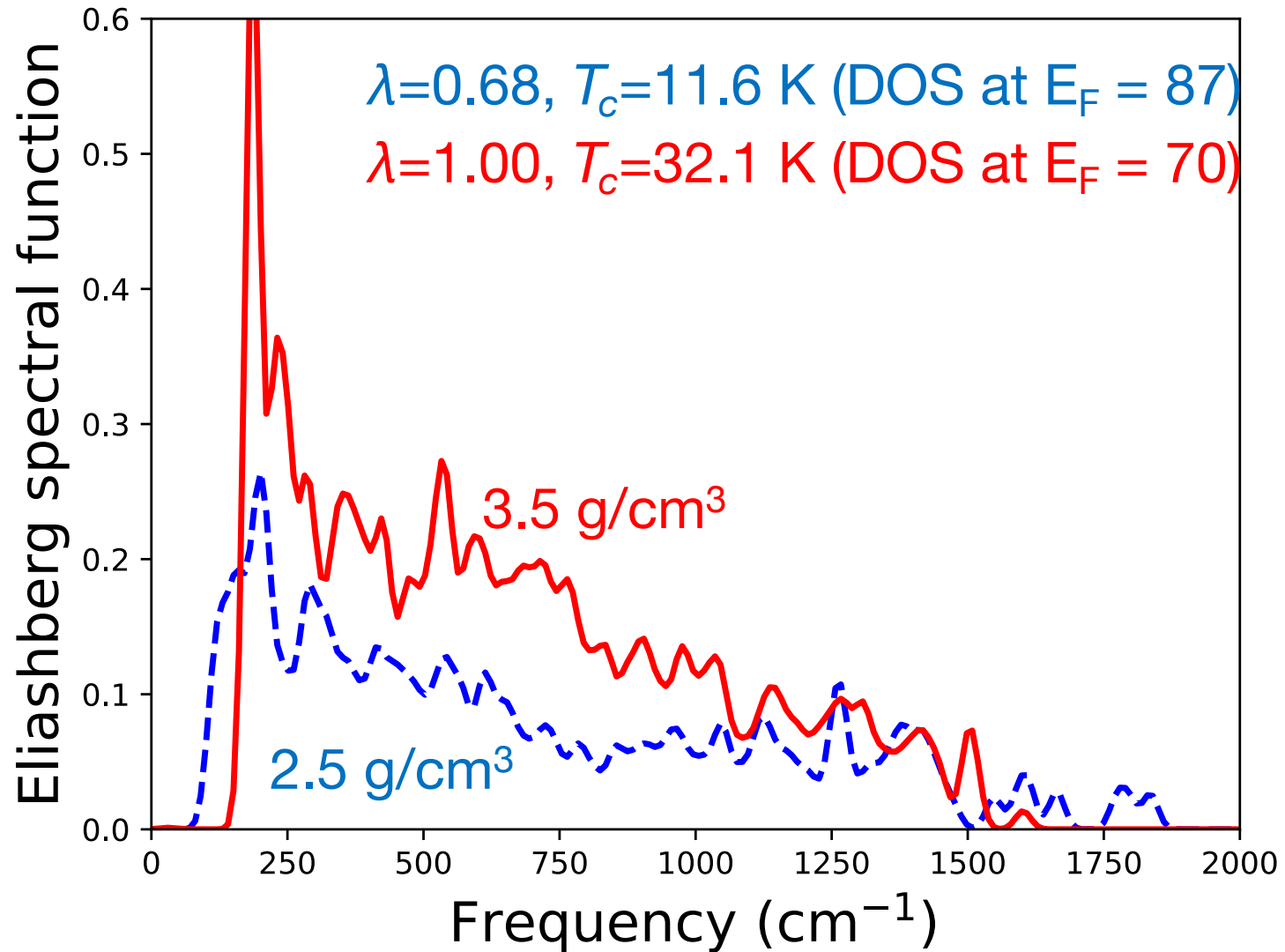
Increased electron-phonon coupling strength  
in entire frequency range upon B doping

# Density of states in 12.5% B-doped case



DOS coming from different components depending on mass densities

# Eliashberg spectral function



Importance of carrier contribution from  $sp^3$  atoms



# Summary

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- Magnetism in amorphous carbon
  - Importance of  $sp^2$ -hybridized atoms
  - High energy in experimental magnetization
  - Small magnetization is possible
- Superconductivity in B-doped amorphous carbon
  - $sp^3$ -hybridized atoms are more important
  - Not inconsistent with experimental studies

**Atomic coordination plays an important role**

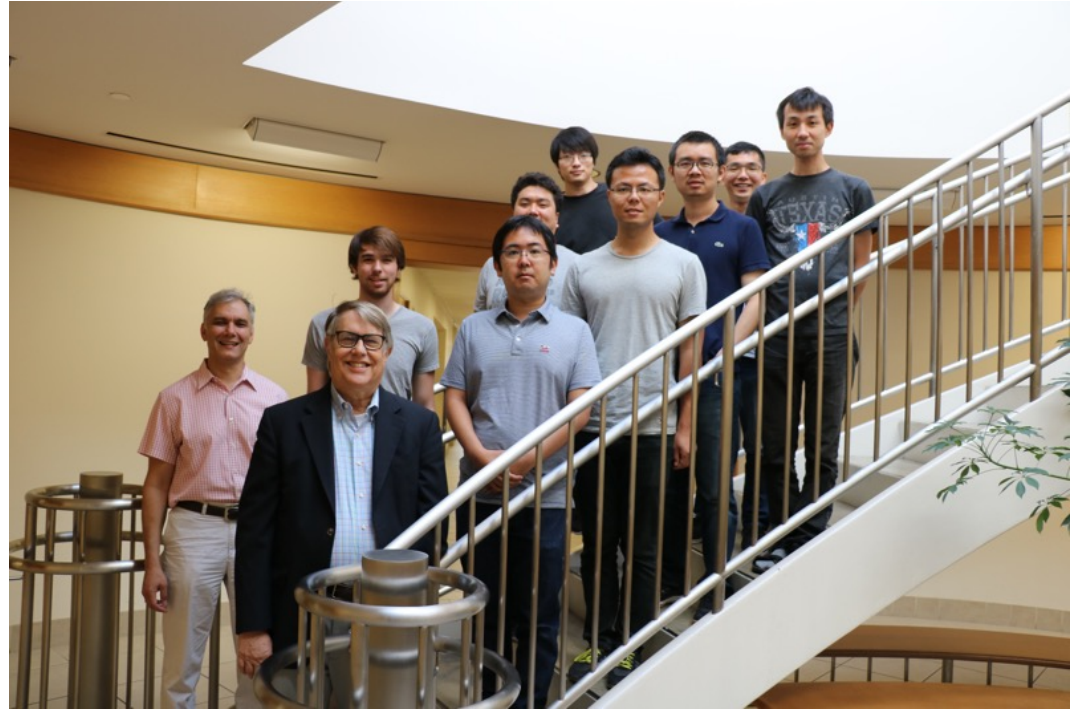
Y. Sakai, J. R. Chelikowsky, and M. L. Cohen, Phys. Rev. B **97**, 054501 (2018)

Y. Sakai, J. R. Chelikowsky, and M. L. Cohen, Phys. Rev. Mater. **2**, 074403 (2018)

# Acknowledgements



Professor Marvin L. Cohen  
(UC Berkeley)



Professor James R. Chelikowsky  
and Chelikowsky group members  
(UT Austin)

# Acknowledgements



**National Energy Research  
Scientific Computing Center**



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