

**Effects of Non-Glide Stresses  
on Plastic Flow and Failure Mechanisms  
arising from Non-Planar Dislocation Core Structures:  
Multiscale Simulations of Non-Associated Flow**

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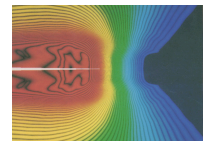
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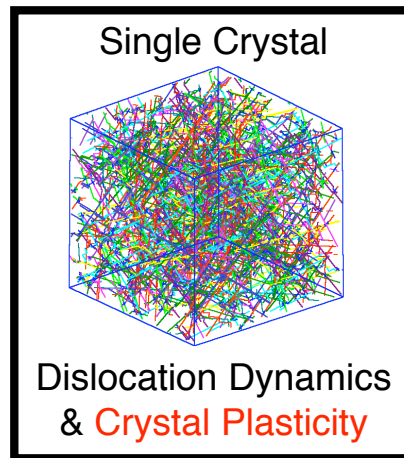
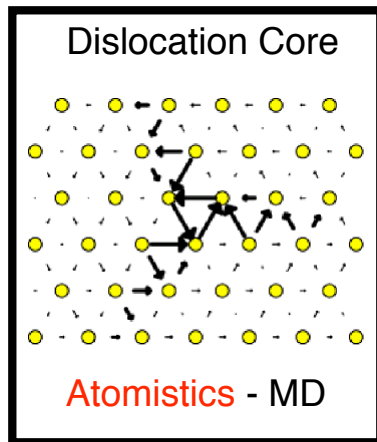
**Mechanics  
of Materials**



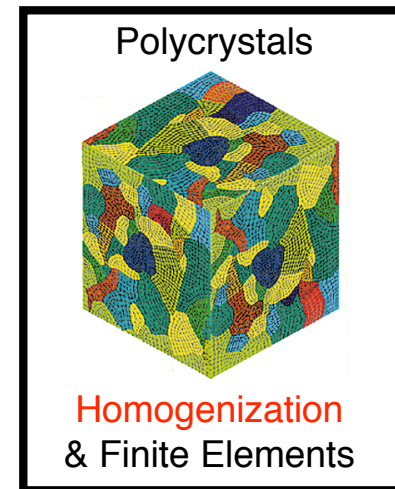
# Multiscale Simulations of Non-Associated Plastic Flow

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- Our strategy is to pass only the most essential information on to higher length scales.

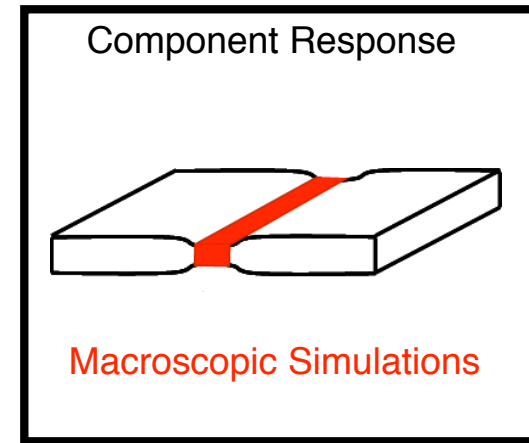
identification of slip planes &  
non-glide stress components



multi-slip models



effective macroscopic behavior

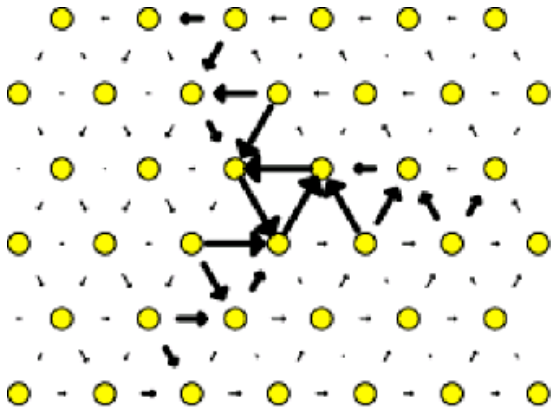


# OVERVIEW

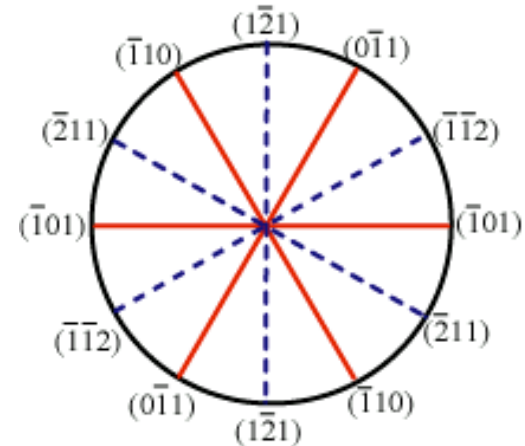
**Using accurate potentials to describe the atomic interactions of BCC metals and intermetallic compounds we have:**

- **studied the influence of the stress state, on the motion of a screw dislocation from atomistic simulations**
- **developed yield criteria for dislocation motion – effects of non-glide stresses on the Peierls barrier**
- **developed multi-slip constitutive equations for single crystals**
- **calculated yield surfaces and flow potentials for polycrystals**
- **derived yield and flow functions for use in *non-associated flow* continuum models of polycrystals**
- **studied implications of non-associated flow on bifurcation modes, forming limits, and cavitation instabilities**

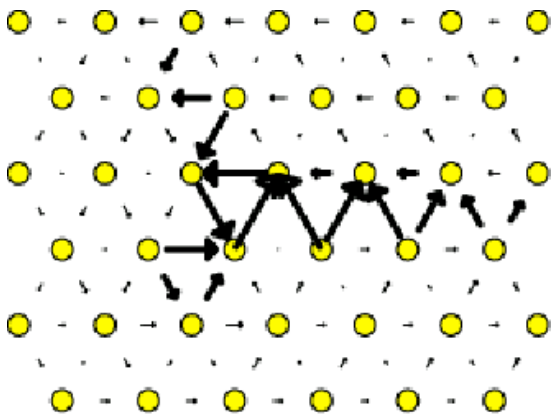
# 1/2[111] Screw Dislocation Core in Mo: Transformations under Applied Stress



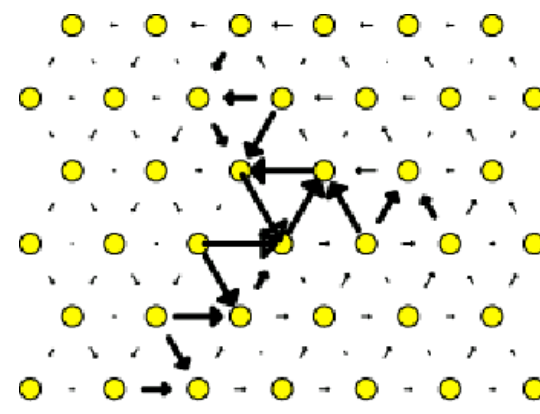
Relaxed Structure: 3-fold symmetry



Planes belonging to the [111] zone



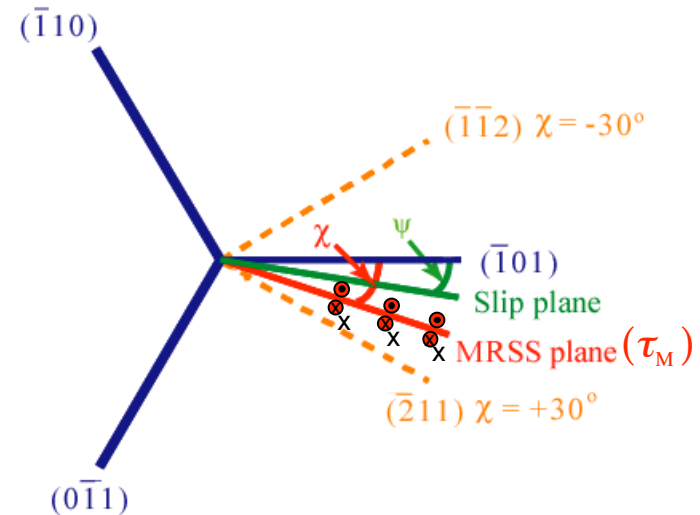
Core under pure shear on  $(\bar{1} \bar{1} 2)$  plane in  $[111]$  direction ( $\chi = -30^\circ$ )



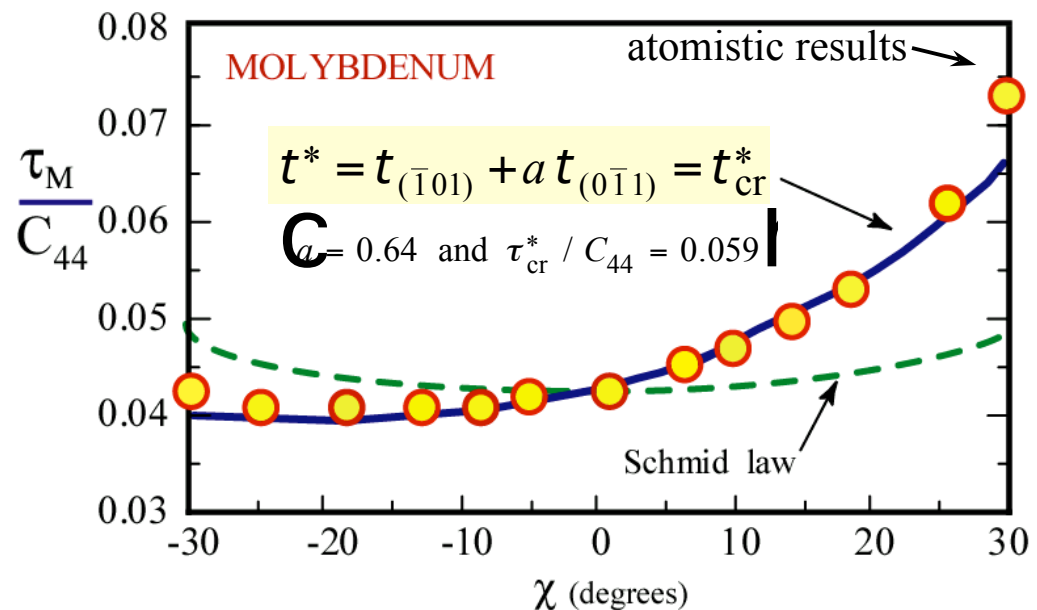
Core under pure shear perpendicular to Burgers vector – **alone this stress cannot move the dislocation**

# Screw Dislocation under Shear Stress on MRSS Plane

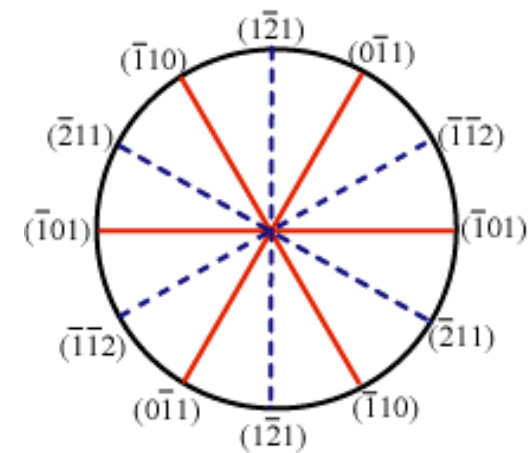
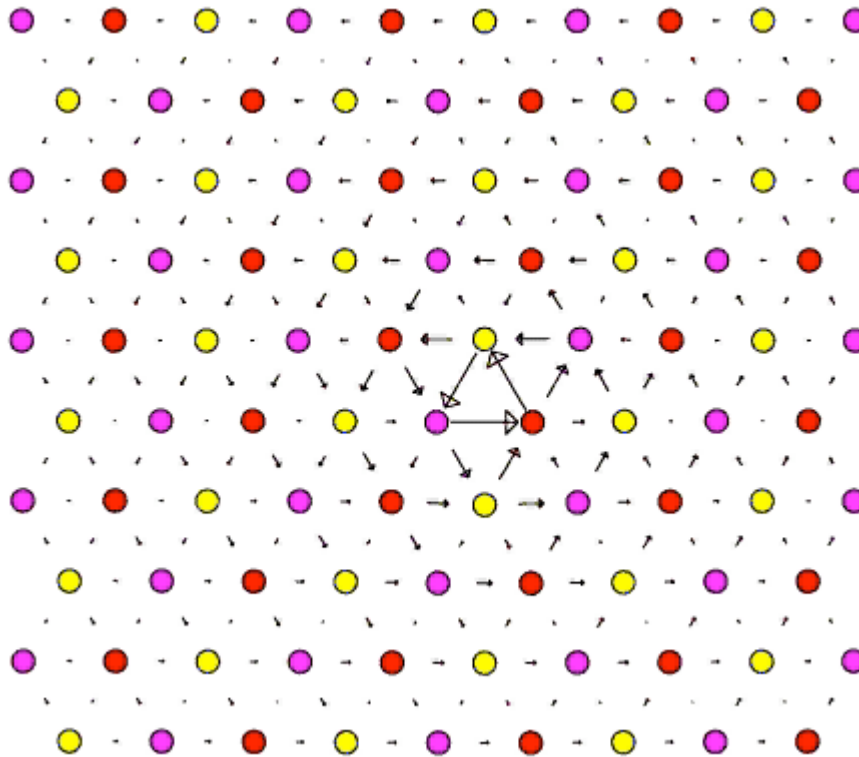
Molybdenum: for  $-30 < \chi < 30$  the dislocation moves on the  $\bar{1}01$  plane at an applied stress (on the MRSSP), but the atomistic results (circles) do not follow Schmid's law:



Other components of shear stress parallel to the Burgers vector affect the dislocation motion, and these can be expressed as a linear combination of the Schmid stress and one other shear stress, e.g.,

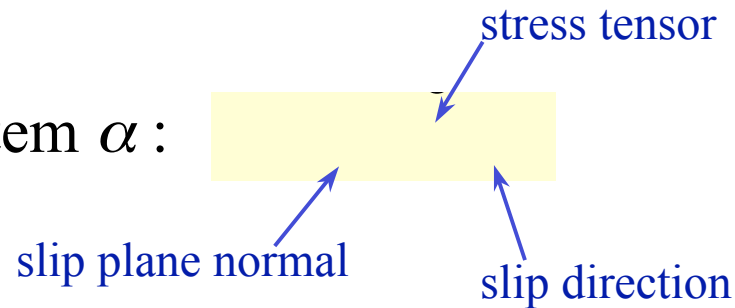


## Motion of a Screw Dislocation in an Infinite Medium Using Bond Order Potentials



# Yield Criteria with non-Glide Stresses

**Schmid stress** on slip system  $\alpha$  :  
(thermodynamic stress)



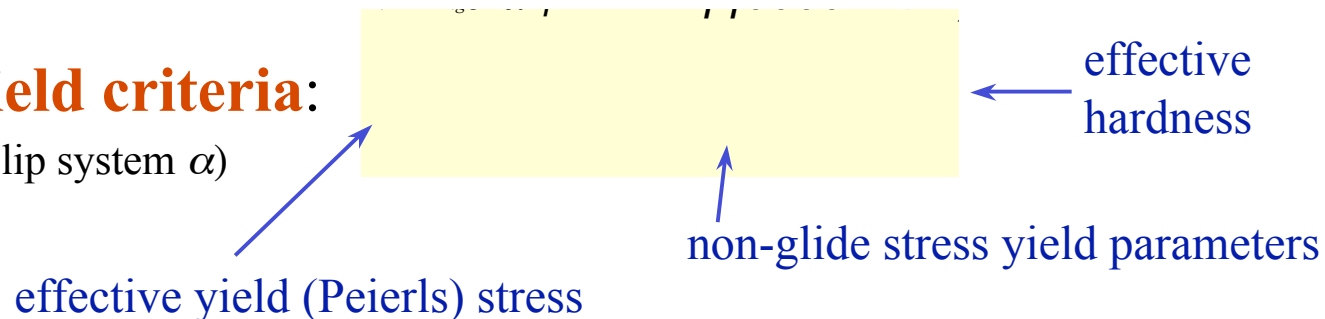
**non-glide stress components:**



where  $\mathbf{n}_\eta^\alpha$  and  $\mathbf{m}_\eta^\alpha$  are crystallographic vectors that resolve each of the  $\eta = 1, N_{ng}$  **non-glide stress components** that **transform dislocation core structures** (both shear and pressure).

**yield criteria:**

(slip system  $\alpha$ )



# Slip Systems for BCC Crystals: the effects of non-glide shear stresses parallel and perpendicular to the Burgers vector

Slip System	Slip Direction	Slip plane	Non-Glide Stress Plane	Slip System	Slip Direction	Slip plane	Non-Glide Stress Plane
$\alpha$	$\mathbf{m}^\alpha$	$\mathbf{n}^\alpha$	$\mathbf{n}_1^\alpha$	$\alpha$	$\mathbf{m}^\alpha$	$\mathbf{n}^\alpha$	$\mathbf{n}_1^\alpha$
1	111	01 $\bar{1}$	$\bar{1}10$	13	$\bar{1}\bar{1}\bar{1}$	01 $\bar{1}$	10 $\bar{1}$
2	111	$\bar{1}01$	0 $\bar{1}1$	14	$\bar{1}\bar{1}\bar{1}$	$\bar{1}01$	$\bar{1}10$
3	111	1 $\bar{1}0$	10 $\bar{1}$	15	$\bar{1}\bar{1}\bar{1}$	1 $\bar{1}0$	0 $\bar{1}1$
4	$\bar{1}11$	0 $\bar{1}1$	101	16	1 $\bar{1}\bar{1}$	0 $\bar{1}1$	$\bar{1}\bar{1}0$
5	$\bar{1}11$	$\bar{1}0\bar{1}$	$\bar{1}\bar{1}0$	17	1 $\bar{1}\bar{1}$	$\bar{1}0\bar{1}$	01 $\bar{1}$
6	$\bar{1}11$	110	01 $\bar{1}$	18	1 $\bar{1}\bar{1}$	110	101
7	$\bar{1}\bar{1}1$	101	011	19	11 $\bar{1}$	101	1 $\bar{1}0$
8	$\bar{1}\bar{1}1$	0 $\bar{1}\bar{1}$	1 $\bar{1}0$	20	11 $\bar{1}$	0 $\bar{1}\bar{1}$	$\bar{1}0\bar{1}$
9	$\bar{1}\bar{1}1$	$\bar{1}10$	$\bar{1}0\bar{1}$	21	11 $\bar{1}$	$\bar{1}10$	011
10	1 $\bar{1}1$	10 $\bar{1}$	110	22	$\bar{1}1\bar{1}$	10 $\bar{1}$	0 $\bar{1}\bar{1}$
11	1 $\bar{1}1$	011	$\bar{1}01$	23	$\bar{1}1\bar{1}$	011	110
12	1 $\bar{1}1$	$\bar{1}\bar{1}0$	0 $\bar{1}\bar{1}$	24	$\bar{1}1\bar{1}$	$\bar{1}\bar{1}0$	$\bar{1}01$

yield criteria:

Schmid stress:

non-glide stresses:



# Multiple Slip in Single Crystals with Non-Glide Stress Effects

yield criteria:

kinematics:

flow rule:

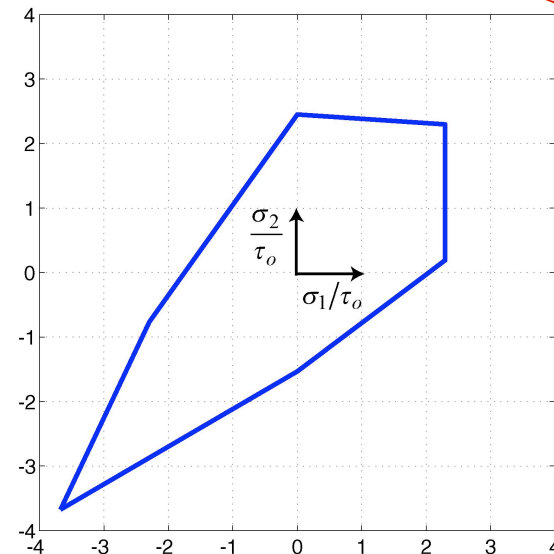
$$(n \gg 1)$$

a non-associated flow theory

BCC yield surface ( $a=0.6$ ) – restricted model

Two-dimensional projection of the yield surface. Euler angles for this crystal orientation are

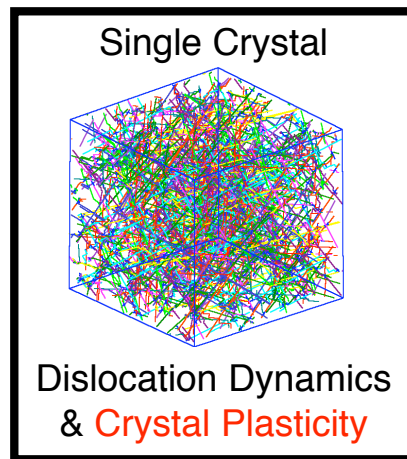
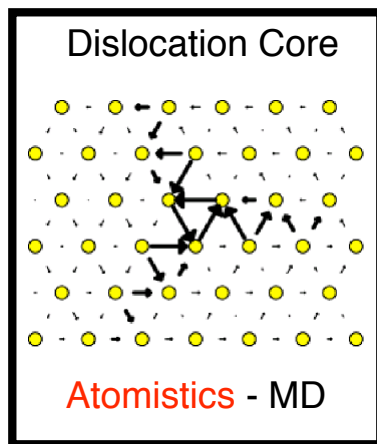
$$\eta, \beta, \phi = (0.785, 2.53, 0)$$



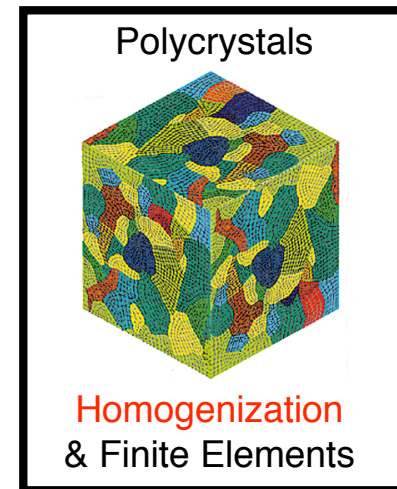
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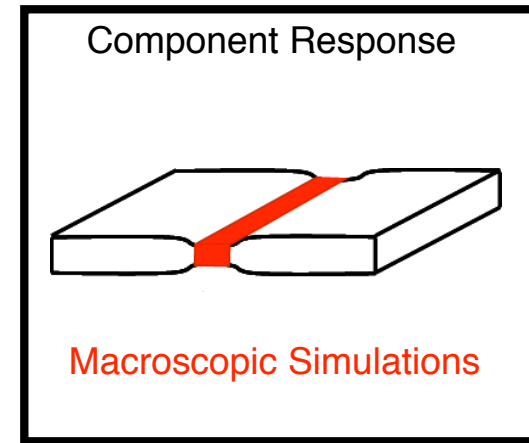
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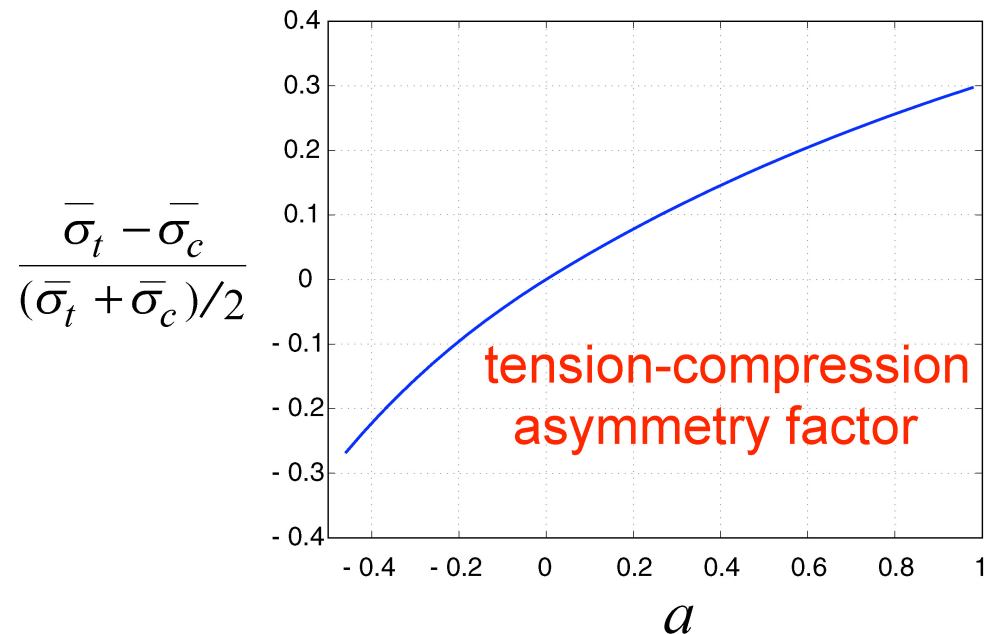
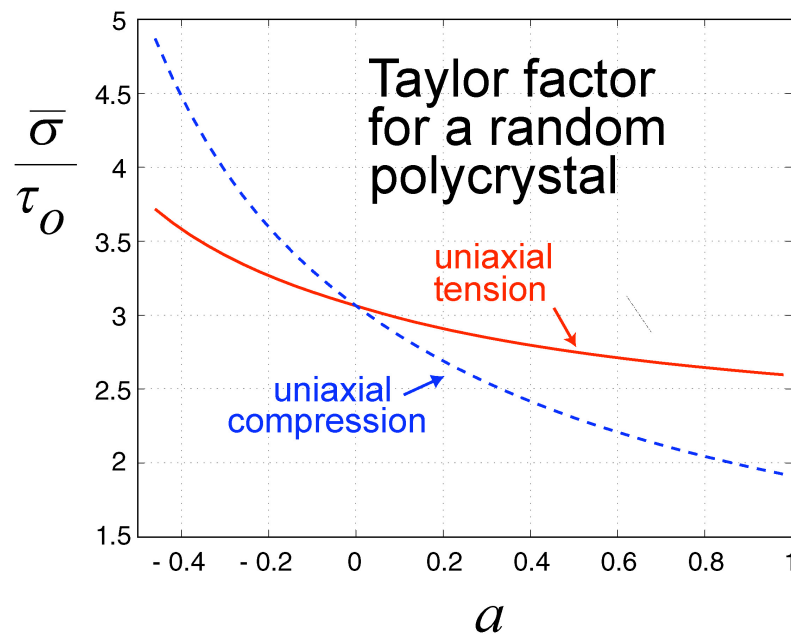


effective macroscopic behavior



# Random BCC Polycrystal with Non-Glide Stresses

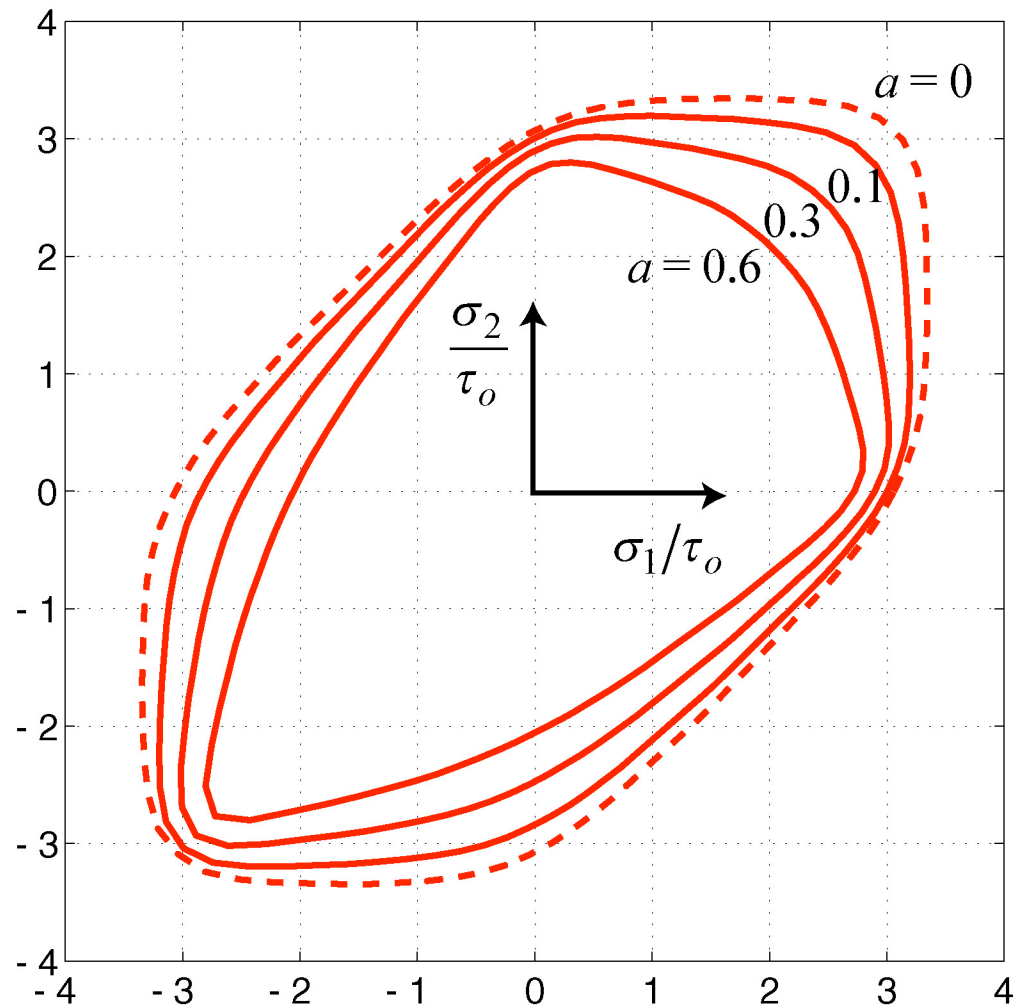
Consider a polycrystal of randomly oriented BCC grains each satisfying the yield criteria:  $\sqrt{\frac{2}{3}} \bar{\sigma} \leq \tau_o$ . Neglecting elastic strains and assuming the strain in each crystal is the same as the macroscopic strain (Taylor hypothesis), a quadratic programming problem is used to solve for the minimum of 5 slips in each crystal, which gives an upper bound to the limit yield surface. For Schmid behavior ( $\alpha=0$ ) the classical Taylor factor is 3.07 times the slip-system yield stress in tension and compression.



## 2D Yield Surfaces for Random BCC Polycrystals

based upon single  
crystal yield criteria  
that include the effects  
of non-glide stresses:

where  $\alpha$  and  $\tau_o$  are  
material parameters



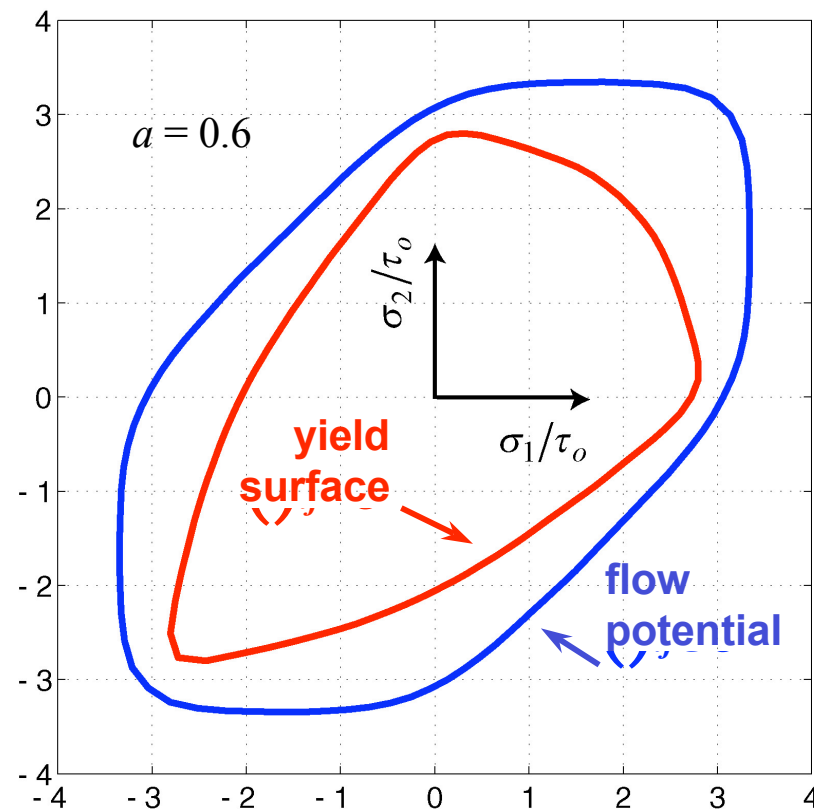
# Non-Associated Flow Behavior macroscopic (engineering) theory

Non-Associated Flow Behavior

$F=G$  for classical  
associated flow  
behavior

plastic strain-rate

These *isotropic* surfaces shown  
are predicted from a Taylor  
model of a random BCC  
polycrystal with single crystal  
yield criteria fitted to atomistic  
calculation of the stress-state  
dependence of the Peierls barrier  
in molybdenum.



# Macroscopic Yield Functions for Random BCC Polycrystals

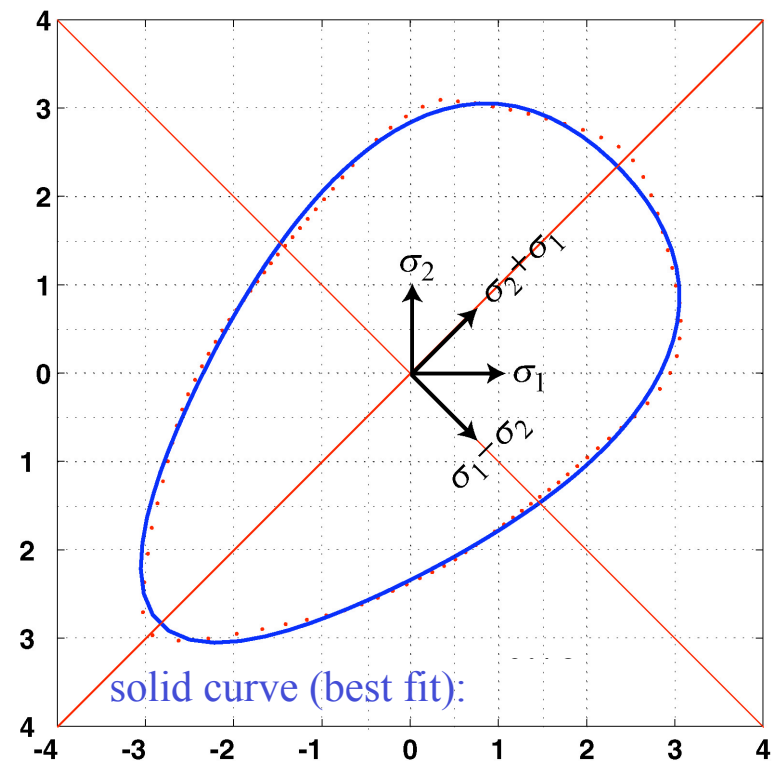
$$\sqrt{\frac{1}{2}(\sigma_1 - \sigma_2)^2 + \frac{1}{2}(\sigma_1 + \sigma_2)^2}$$

$$\sqrt{\frac{1}{2}(\sigma_1 - \sigma_2)^2 + \frac{1}{2}(\sigma_1 + \sigma_2)^2}$$

Yield stress in tension

Yield stress in compression

note: reduces to  
the von Mises surface



points plotted are from Taylor calculation for BCC polycrystal with *the effects of non-glide stresses both parallel to and perpendicular to the Burgers vector*

# Macroscopic Flow Potentials for Random BCC Polycrystals

$$\sqrt{\frac{1}{2}(\sigma_1 - \sigma_2)^2}$$

$G$  is the flow potential:

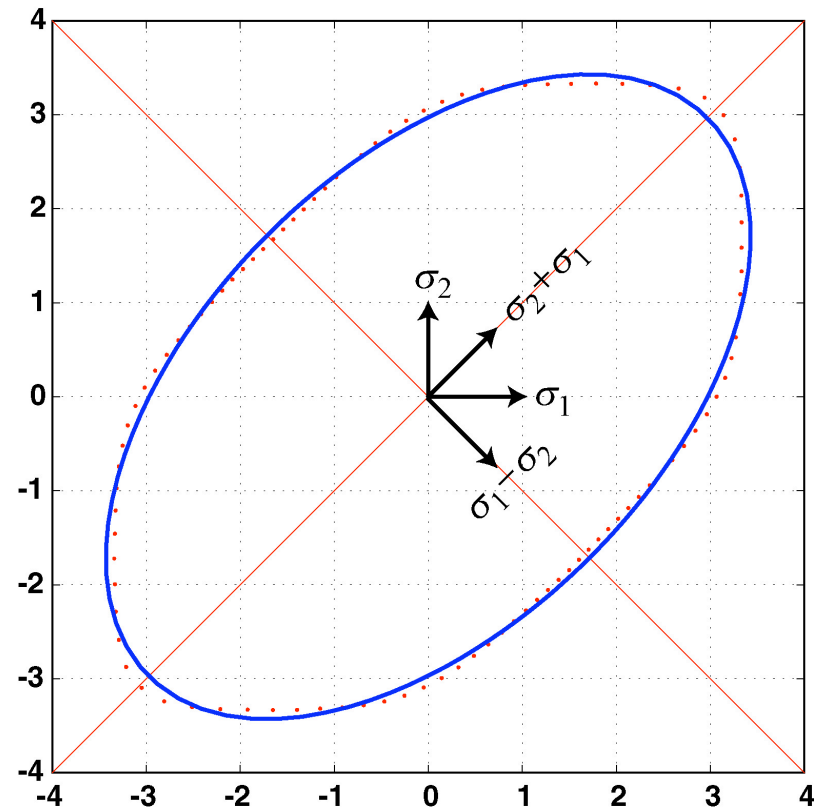
$$G = \frac{1}{2}(\sigma_1 - \sigma_2)^2$$

hardening law:

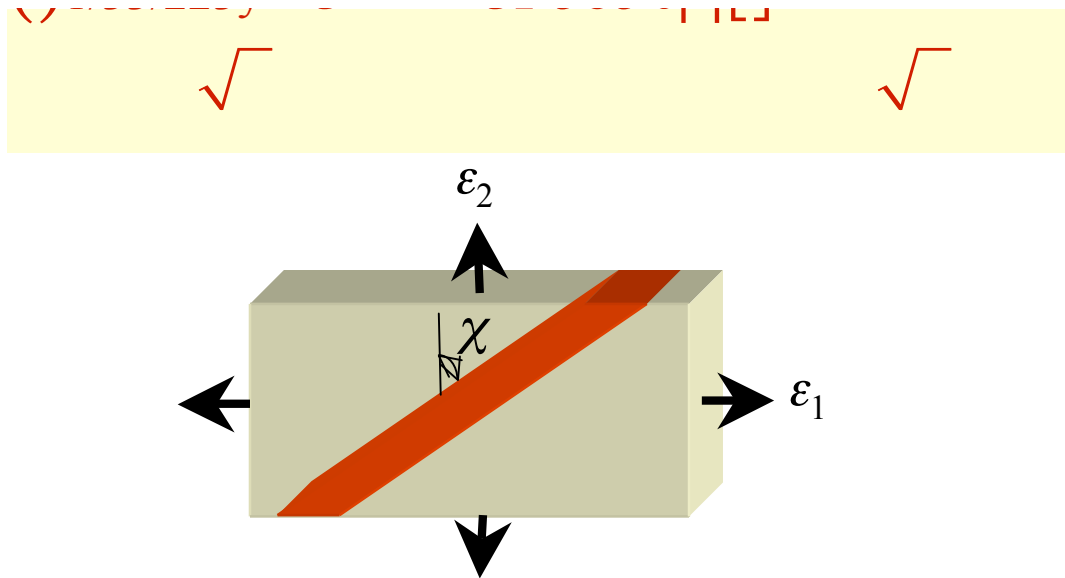
$$\sigma = \sigma_0 + K \epsilon^n$$

solid curve (best fit):

points plotted are from Taylor calculation for BCC polycrystal

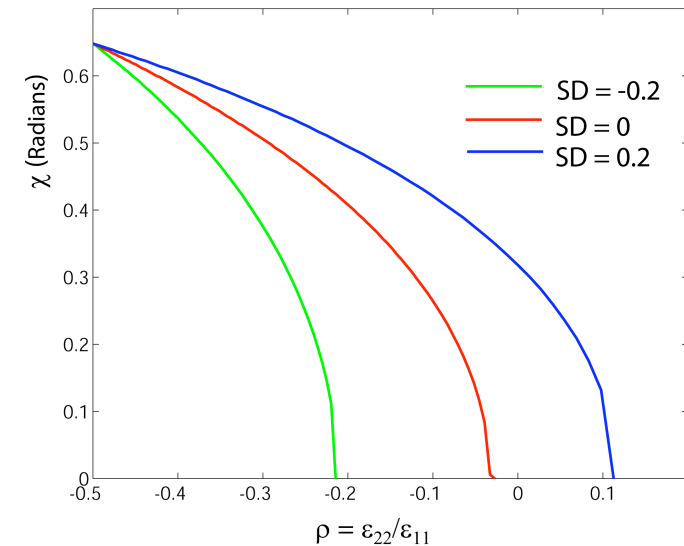
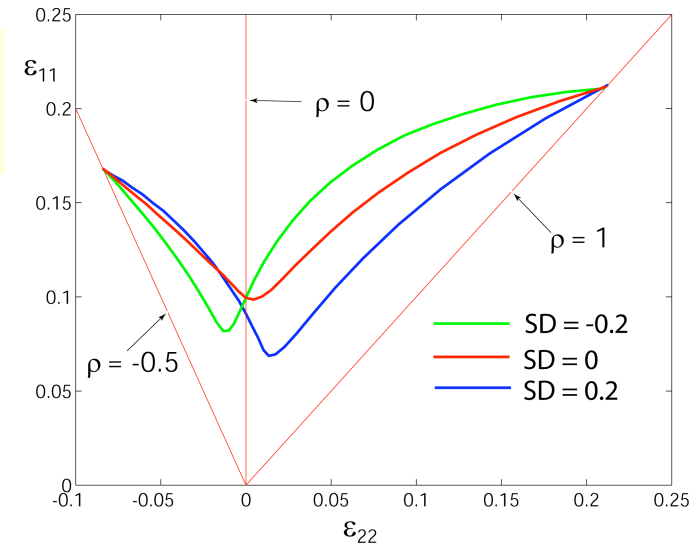


# Effects of Non-Associated Flow on Bifurcations from Homogeneous Plane Stress Loading States



If  $\Delta \mathbf{D}$  represents the jump in strain rate across the band (shown in red) and  $\mathbf{C}$  the incremental modulus. The bifurcation condition is given by

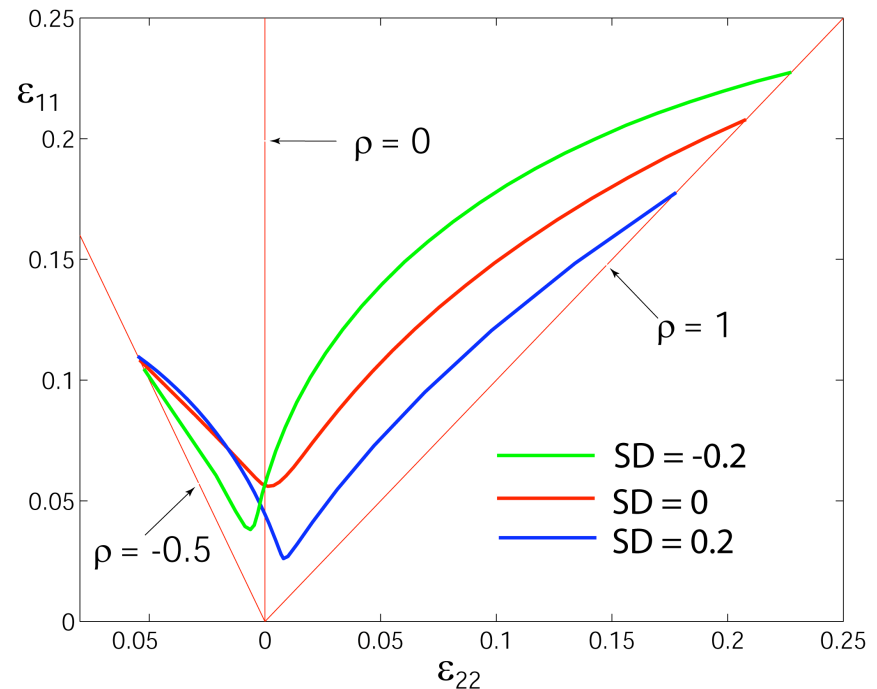
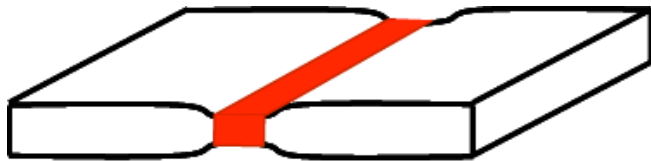
$$\Delta \mathbf{D} : \mathbf{C} : \Delta \mathbf{D} = 0$$





## Effects of Non-Associated Flow on Forming Limits

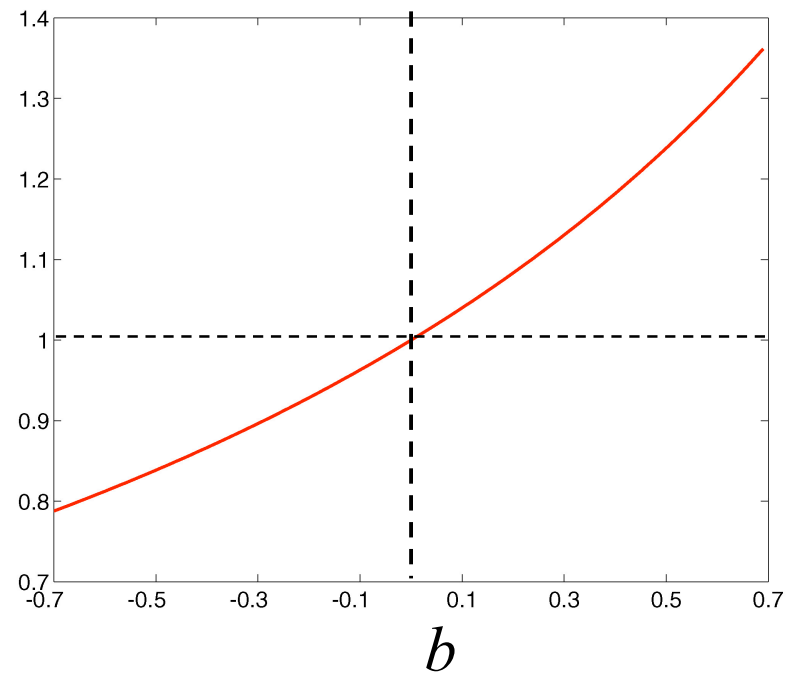
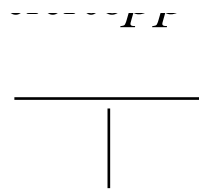
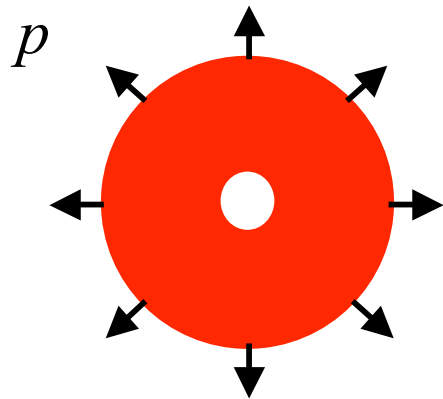
Sheet necking under  
biaxial straining



MK analysis of **sheet necking** using deformation theory for strain hardening coefficients of  $N = 0.1$ .

# Effects of Non-Associated Flow on Cavitation Instabilities

critical pressure at  
unstable cavity growth



# CONCLUSIONS

- From the multiscale simulations beginning with the input from atomistics we observe that the non-glide stresses have similar order-of-magnitude effects at single and polycrystal levels and generally on macroscopic response.
- Since these effects have their origin in dislocation core transformations, they arise generally at high stress levels, particularly at high strain-rates and/or low temperatures.
- There are comparable order-of-magnitude effects on *strain localization* in the form of bifurcations, sheet necking, and on cavitation instabilities to name a few.
- In the language of continuum plasticity, at each scale a significant effect of *non-associated flow behavior* is present.